AI GERRA I

Lesson 8: Adding and Subtracting Polynomials

Classwork

Exercise 1

- a. How many quarters, nickels, and pennies are needed to make \$1.13?
- b. Fill in the blanks:

$$8,943 = \underline{\hspace{1cm}} \times 1000 + \underline{\hspace{1cm}} \times 100 + \underline{\hspace{1cm}} \times 10 + \underline{\hspace{1cm}} \times 1$$

$$= \underline{\hspace{1cm}} \times 10^{3} + \underline{\hspace{1cm}} \times 10^{2} + \underline{\hspace{1cm}} \times 10 + \underline{\hspace{1cm}} \times 1$$

c. Fill in the blanks:

$$8,943 = \underline{\hspace{1cm}} \times 20^3 + \underline{\hspace{1cm}} \times 20^2 + \underline{\hspace{1cm}} \times 20 + \underline{\hspace{1cm}} \times 1$$

d. Fill in the blanks:

$$113 = \underline{\hspace{1cm}} \times 5^2 + \underline{\hspace{1cm}} \times 5 + \underline{\hspace{1cm}} \times 1$$

Exercise 2

Now let's be as general as possible by not identifying which base we are in. Just call the base x.

Consider the expression $1 \times x^3 + 2 \times x^2 + 7 \times x + 3 \times 1$, or equivalently $x^3 + 2x^2 + 7x + 3$.

- a. What is the value of this expression if x = 10?
- b. What is the value of this expression if x = 20?



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Exercise 3

a. When writing numbers in base 10, we only allow coefficients of 0 through 9. Why is that?

b. What is the value of 22x + 3 when x = 5? How much money is 22 nickels and 3 pennies?

c. What number is represented by $4x^2 + 17x + 2$ if x = 10?

d. What number is represented by $4x^2 + 17x + 2$ if x = -2 or if $x = \frac{2}{3}$?

e. What number is represented by $-3x^2 + \overline{2}x + \frac{1}{2}$ when $x = \overline{2}$?

Polynomial Expression: A polynomial expression is either

- 1. A numerical expression or a variable symbol, or
- 2. The result of placing two previously generated polynomial expressions into the blanks of the addition operator (__+__) or the multiplication operator (__×__).



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Exercise 4

Find each sum or difference by combining the parts that are alike.

- a. 417 + 231 = _____hundreds + _____tens + _____ones + ____hundreds + _____tens + _____ones = _____hundreds + _____tens + _____ones
- b. $4x^2 + x + 7 + (2x^2 + 3x + 1)$
- c. $3x^3 x^2 + 8 (x^3 + 5x^2 + 4x 7)$
- d. $3x^3 + 8x 2x^3 + 12$
- e. $5-t-t^2+(9t+t^2)$
- f. 3p+1+6p-8-(p+2)

Lesson Summary

A <u>monomial</u> is a polynomial expression generated using only the multiplication operator ($\underline{} \times \underline{}$). Thus, it does not contain + or - operators. Monomials are written with numerical factors multiplied together and variable or other symbols each occurring one time (using exponents to condense multiple instances of the same variable).

A **polynomial** is the sum (or difference) of monomials.

The <u>degree of a monomial</u> is the sum of the exponents of the variable symbols that appear in the monomial.

The <u>degree of a polynomial</u> is the degree of the monomial term with the highest degree.

Problem Set

1. Celina says that each of the following expressions is actually a binomial in disguise:

i.
$$5abc - 2a^2 + 6abc$$

ii.
$$5x^3 \cdot 2x^2 - 10x^4 + 3x^5 + 3x \cdot -2 x^4$$

iii.
$$t + 2^2 - 4t$$

iv.
$$5 a - 1 - 10(a - 1) + 100(a - 1)$$

v.
$$2\pi r - \pi r^2 r - (2\pi r - \pi r^2) \cdot 2r$$

For example, she sees that the expression in (i) is algebraically equivalent to $11abc - 2a^2$, which is indeed a binomial. (She is happy to write this as $11abc + -2a^2$, if you prefer.)

Is she right about the remaining four expressions?

- 2. Janie writes a polynomial expression using only one variable, x, with degree 3. Max writes a polynomial expression using only one variable, x, with degree 7.
 - a. What can you determine about the degree of the sum of Janie's and Max's polynomials?
 - b. What can you determine about the degree of the difference of Janie's and Max's polynomials?
- 3. Suppose Janie writes a polynomial expression using only one variable, x, with degree of 5, and Max writes a polynomial expression using only one variable, x, with degree of 5.
 - a. What can you determine about the degree of the sum of Janie's and Max's polynomials?
 - b. What can you determine about the degree of the difference of Janie's and Max's polynomials?
- 4. Find each sum or difference by combining the parts that are alike.

a.
$$2p+4+5p-1-(p+7)$$

b.
$$7x^4 + 9x - 2(x^4 + 13)$$

c.
$$6-t-t^4+(9t+t^4)$$

d.
$$5-t^2+6$$
 $t^2-8-(t^2+12)$

e.
$$8x^3 + 5x - 3(x^3 + 2)$$

f.
$$12x + 1 + 2x - 4 - (x - 15)$$

g.
$$13x^2 + 5x - 2(x^2 + 1)$$

h.
$$9-t-t^2-\frac{3}{2} 8t+2t^2$$

i.
$$4m+6-12 m-3+m+2$$

j.
$$15x^4 + 10x - 12(x^4 + 4x)$$