

# **Lesson 12: Solving Equations**

#### **Classwork**

#### **Opening Exercise**

Answer the following questions.

- a. Why should the equations x 1 x + 3 = 17 + x and x 1 x + 3 = x + 17 have the same solution set?
- b. Why should the equations x 1 x + 3 = 17 + x and x + 3 x 1 = 17 + x have the same solution set?
- c. Do you think the equations (x 1)(x + 3) = 17 + x and x 1 x + 3 + 500 = 517 + x should have the same solution set? Why?
- d. Do you think the equations x 1 x + 3 = 17 + x and 3(x 1)(x + 3) = 51 + 3x should have the same solution set? Explain why.

#### Exercise 1

- a. Use the commutative property to write an equation that has the same solution set as  $x^{2} - 3x + 4 = (x + 7)(x - 12)(5)$
- b. Use the associative property to write an equation that has the same solution set as  $x^{2} - 3x + 4 = (x + 7)(x - 12)(5)$
- c. Does this reasoning apply to the distributive property as well?





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### Exercise 2

Consider the equation  $x^2 + 1 = 7 - x$ .

- a. Verify that this has the solution set  $\{-3, 2\}$ . Draw this solution set as a graph on the number line. We will later learn how to show that these happen to be the ONLY solutions to this equation.
- Let's add four to both sides of the equation and consider the new equation  $x^2 + 5 = 11 x$ . Verify 2 and -3b. are still solutions.
- Let's now add x to both sides of the equation and consider the new equation  $x^2 + 5 + x = 11$ . Are 2 and -3c. still solutions?
- d. Let's add -5 to both sides of the equation and consider the new equation  $x^2 + x = 6$ . Are 2 and -3 still solutions?

e. Let's multiply both sides by  $\frac{1}{6}$  to get  $\frac{x^2 + x}{6} = 1$ . Are 2 and -3 still solutions?

f. Let's go back to part (d) and add  $3x^3$  to both sides of the equation and consider the new equation  $x^{2} + x + 3x^{3} = 6 + 3x^{3}$ . Are 2 and -3 still solutions?





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### Exercise 3

a. Solve for 
$$r: \frac{3}{2r} = \frac{1}{4}$$
 b. Solve for  $s: s^2 + 5 = 30$  c. Solve for  $y: 4y - 3 = 5y - 8$ 

## **Exercise 4**

Consider the equation 3x + 4 = 8x - 16. Solve for x using the given starting point.

Group 1	Group 2	Group 3	Group 4
Subtract 3x from both sides	Subtract 4 from both sides	Subtract 8x from both sides	Add 16 to both sides







#### **Closing Exercise**

Consider the equation  $3x^2 + x = x - 2 x + 5 x$ .

- Use the commutative property to create an equation with the same solution set. a.
- b. Using the result from (a), use the associative property to create an equation with the same solution set.
- Using the result from (b), use the distributive property to create an equation with the same solution set. с.
- Using the result from (c), add a number to both sides of the equation. d.
- Using the result from (d), subtract a number from both sides of the equation. e.
- f. Using the result from (e), multiply both sides of the equation by a number.
- Using the result from (f), divide both sides of the equation by a number. g.
- What do all seven equations have in common? Justify your answer. h.





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#### **Lesson Summary**

If x is a solution to an equation, it will also be a solution to the new equation formed when the same number is added to (or subtracted from) each side of the original equation or when the two sides of the original equation are multiplied by (or divided by) the same non-zero number. These are referred to as the *Properties of Equality*.

If one is faced with the task of solving an equation, that is, finding the solution set of the equation:

Use the *commutative, associative,* and *distributive properties,* AND use the *properties of equality* (adding, subtracting, multiplying by non-zeros, dividing by non-zeros) to keep rewriting the equation into one whose <u>solution set you easily recognize</u>. (We believe that the solution set <u>will not change</u> under <u>these</u> operations.)

## **Problem Set**

1. Which of the following equations have the same solution set? Give reasons for your answers that do not depend on solving the equations.

I. $x - 5 = 3x + 7$	II. $3x - 6 = 7x + 8$	III. $15x - 9 = 6x + 24$
IV. $6x - 16 = 14x + 12$	V. $9x + 21 = 3x - 15$	VI. $-0.05 + \frac{x}{100} = \frac{3x}{100} + 0.07$

Solve the following equations, check your solutions, and then graph the solution sets.

2. $-16 - 6v = -2(8v - 7)$	3. $2(6b+8) = 4+6b$	4. $x^2 - 4x + 4 = 0$
5. $7 - 8x = 7(1 + 7x)$	6. $39 - 8n = -8(3 + 4n) + 3n$	7. $x - 1$ $x + 5 = x^2 + 4x - 2$
8. $x^2 - 7 = x^2 - 6x - 7$	9. $-7 - 6a + 5a = 3a - 5a$	10. $7 - 2x = 1 - 5x + 2x$
11. 4 $x - 2 = 8 x - 3 - 12$	12. $-3 \ 1-n = -6 - 6n$	13. $-21 - 8a = -5(a + 6)$
14. $-11 - 2p = 6p + 5(p + 3)$	15. $\frac{x}{x+2} = 4$	16. $2 + \frac{x}{9} = \frac{x}{3} - 3$
17. $-5 -5x - 6 = -22 - x$	18. $\frac{x+4}{3} = \frac{x+2}{5}$	19. $-5 \ 2r - 0.3 \ + 0.5 \ 4r + 3 \ = -64$





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