

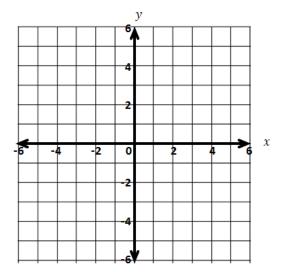
Lesson 16: Graphs Can Solve Equations Too

Classwork

Opening Exercise

1. Solve for x in the following equation: |x + 2| - 3 = 0.5x + 1.

- 2. Now let f(x) = |x + 2| 3 and g(x) = 0.5x + 1. When does f(x) = g(x)?
 - a. Graph y = f(x) and y = g(x) on the same set of axes.
 - b. When does f(x) = g(x)? What is the visual significance of the points where f(x) = g(x)?



c. Is each intersection point (x, y) an element of the graph f and an element of the graph of g? In other words, do the functions f and g really have the same value when x = 4? What about when x = -4?



Graphs Can Solve Equations Too 10/30/14

engage^{ny}

S.102



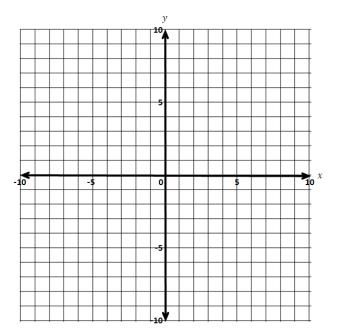
Example 1

Solve this equation by graphing two functions on the same Cartesian plane: -|x - 3| + 4 = |0.5x| - 5.

Let f(x) = -|x - 3| + 4 and let g(x) = |0.5x| - 5 where x can be any real number.

We are looking for values of x at which the functions f and g have the same output value.

Therefore, we set y = f(x) and y = g(x) so we can plot the graphs on the same coordinate plane:



From the graph, we see that the two intersection points are ______ and ______.

The fact that the graphs of the functions meet at these two points means that when x is _____ both f(x) and g(x)

are _____, or when x is _____ both f(x) and g(x) are _____.

Thus, the expressions -|x - 3| + 4 and |0.5x| - 5 are equal when x =_____ or when x =_____.

Therefore, the solution set to the original equation is ______.



Graphs Can Solve Equations Too 10/30/14



engage^{ny}

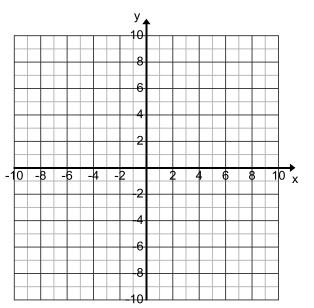


Example 2

Solve this equation graphically: -|x - 3.5| + 4 = -0.25x - 1.

a. Write the two functions represented by each side of the equation.

b. Graph the functions in an appropriate viewing window.



- c. Determine the intersection points of the two functions.
- d. Verify that the *x*-coordinates of the intersection points are solutions to the equation.



Graphs Can Solve Equations Too 10/30/14



engage^{ny}

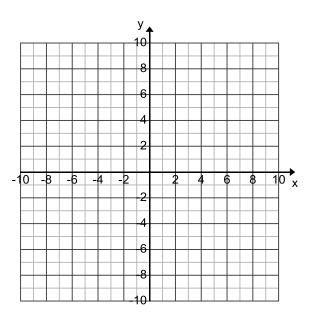


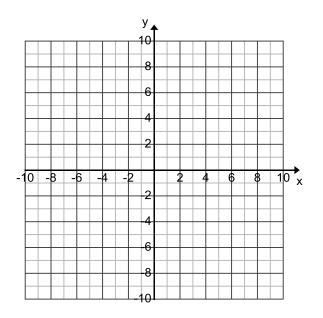
Exercises 1–5

Use graphs to find approximate values of the solution set for each equation. Use technology to support your work. Explain how each of your solutions relates to the graph. Check your solutions using the equation.

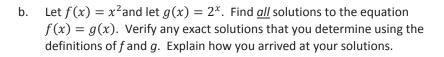
1. 3 - 2x = |x - 5|

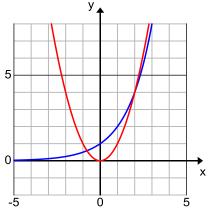
2. $2(1.5)^x = 2 + 1.5x$





- 3. The graphs of the functions f and g are shown.
 - a. Use the graphs to *approximate* the solution(s) to the equation f(x) = g(x).







Graphs Can Solve Equations Too 10/30/14

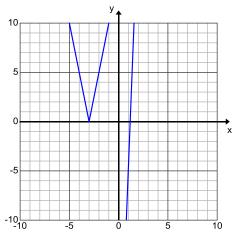


S.105

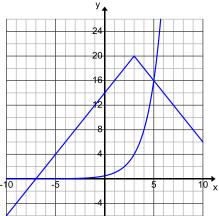




4. The graphs of f, a function that involves taking an absolute value, and g, a linear function, are shown to the right. Both functions are defined over all real values for x. Tami concluded that the equation f(x) = g(x) has no solution. Do you agree or disagree? Explain your reasoning.



5. The graphs of f (a function that involves taking the absolute value) and g (an exponential function) are shown below. Sharon said the solution set to the equation f(x) = g(x) is exactly {-7,5}.
Do you agree or disagree with Sharon? Explain your reasoning.





Graphs Can Solve Equations Too 10/30/14

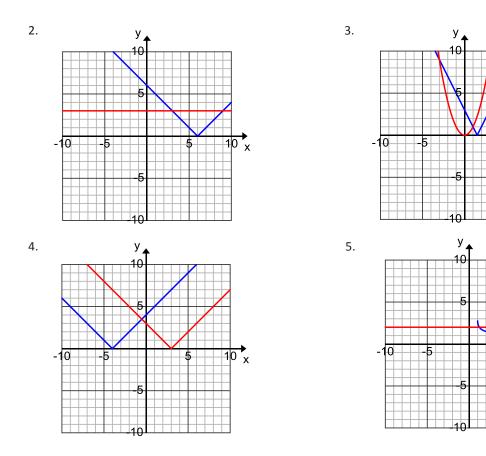
engage^{ny}



Problem Set

- 1. Solve the following equations graphically. Verify the solution sets using the original equations.
 - a. $2x 4 = \sqrt{x + 5}$
 - b. $|x| = x^2$
 - c. $x + 2 = x^3 2x 4$
 - d. |3x 4| = 5 |x 2|
 - e. $0.5x^3 4 = 3x + 1$
 - f. $6\left(\frac{1}{2}\right)^{5x} = 10 6x$

In each problem, the graphs of the functions f and g are shown on the same Cartesian plane. Estimate the solution set to the equation f(x) = g(x). Assume that the graphs of the two functions only intersect at the points shown on the graph.





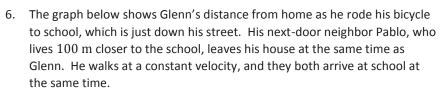
Lesson 16: Date: Graphs Can Solve Equations Too 10/30/14



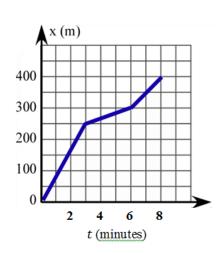


10 x

10 x



- a. Graph a linear function that represents Pablo's distance from Glenn's home as a function of time.
- b. Estimate when the two boys pass each other.
- c. Write piecewise-linear functions to represent each boy's distance and use them to verify your answer to part (b).



Lesson 16

M3

ALGEBRA I



Graphs Can Solve Equations Too 10/30/14

enga



S.108

