

## Lesson 14: Similarity

### Classwork

#### Example 1

We said that for a figure  $A$  in the plane, it must be true that  $A \sim A$ . Describe why this must be true.

#### Example 2

We said that for figures  $A$  and  $B$  in the plane so that  $A \sim B$ , then it must be true that  $B \sim A$ . Describe why this must be true.

#### Example 3

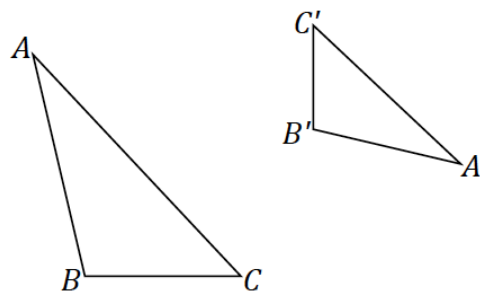
Based on the definition of *similar*, how would you show that any two circles are similar?

**Example 4**

Suppose  $\triangle ABC \leftrightarrow \triangle DEF$  and under this correspondence, corresponding angles are equal and corresponding sides are proportional. Does this guarantee that  $\triangle ABC$  and  $\triangle DEF$  are similar?

**Example 5**

- a. In the diagram below,  $\triangle ABC \sim \triangle A'B'C'$ . Describe a similarity transformation that maps  $\triangle ABC$  to  $\triangle A'B'C'$ .



- b. Joel says the sequence must require a dilation and three rigid motions, but Sharon is sure there is a similarity composed of just a dilation and just two rigid motions. Who is right?

**Lesson Summary**

Similarity is reflexive because a figure is similar to itself.

Similarity is symmetric because once a similarity transformation is determined to take a figure to another, there are inverse transformations that will take the figure back to the original.

**Problem Set**

1. If you are given any two congruent triangles, describe a sequence of basic rigid motions that will take one to the other.
2. If you are given two similar triangles that are not congruent triangles, describe a sequence of dilations and basic rigid motions that will take one to the other.
3. Given two line segments,  $\overline{AB}$  and  $\overline{CD}$ , of different lengths, answer the following questions.
  - a. It is always possible to find a similarity transformation that maps  $\overline{AB}$  to  $\overline{CD}$  sending  $A$  to  $C$  and  $B$  to  $D$ . Describe one such similarity transformation.
  - b. If you are given that  $\overline{AB}$  and  $\overline{CD}$  are not parallel, are not congruent, do not share any points, and do not lie in the same line, what is the least number of transformations needed in a sequence to map  $\overline{AB}$  to  $\overline{CD}$ ? Which transformations make this work?
  - c. If you performed a similarity transformation that instead takes  $A$  to  $D$  and  $B$  to  $C$ , either describe what mistake was made in the similarity transformation, or describe what additional transformation is needed to fix the error so that  $A$  maps to  $C$  and  $B$  maps to  $D$ .
4. We claim that similarity is transitive, i.e., that if  $A$ ,  $B$ , and  $C$  are figures in the plane such that  $A \sim B$  and  $B \sim C$ , then  $A \sim C$ . Describe why this must be true.
5. Given two line segments,  $\overline{AB}$  and  $\overline{CD}$ , of different lengths, we have seen that it is always possible to find a similarity transformation that maps  $\overline{AB}$  to  $\overline{CD}$ , sending  $A$  to  $C$  and  $B$  to  $D$  with one rotation and one dilation. Can you do this with one reflection and one dilation?
6. Given two triangles,  $\triangle ABC \sim \triangle DEF$ , is it always possible to rotate  $\triangle ABC$  so that the sides of  $\triangle ABC$  are parallel to the corresponding sides in  $\triangle DEF$ ; i.e.,  $\overline{AB} \parallel \overline{DE}$ , etc.?