## Lesson 1: What Is Area?

## Classwork

## Exploratory Challenge 1

a. What is area?
b. What is the area of the rectangle below whose side lengths measure 3 units by 5 units?

c. What is the area of the $\frac{3}{4} \times \frac{5}{3}$ rectangle below?


## Exploratory Challenge 2

a. What is the area of the rectangle below whose side lengths measure $\sqrt{3}$ units by $\sqrt{2}$ units? Use the unit squares on the graph to guide your approximation. Explain how you determined your answer.

b. Is your answer precise?

## Discussion

Use Figures 1, 2, and 3 to find upper and lower approximations of the given rectangle.

Figure 1


Figure 2


Figure 3


| Lower Approximations |  |  |
| :---: | :---: | :---: |
| Less than $\sqrt{2}$ | Less than $\sqrt{3}$ | Less than or equal to $A$ |
| 1 | 1 | $1 \times 1=$ |
|  | 1.7 | $\times 1.7=$ |
| 1.41 | 1.732 | $1.41 \times$ |
| 1.414 | 1.7320 | $1.414 \times 1.732=$ |
| 1.4142 |  | $=4948 \times 1.7320=49344$ |
|  |  | $1.414213 \times 1.732050=4948762665$ |
| 1.414213 |  |  |


| Upper Approximations |  |  |
| :---: | :---: | :---: |
| Greater than $\sqrt{2}$ | Greater than $\sqrt{3}$ | Greater than or equal to $A$ |
| 2 | 2 | $2 \times 2=4$ |
| 1.5 | 1.8 | $1.5 \times 1.8=$ |
| 1.42 | 1.74 | $1.42 \times 1.74=2.4708$ |
|  | 1.733 | $\times 1.733=$ |
| 1.4143 | 1.7321 | $1.4143 \times 1.7321=2.44970903$ |
| 1.41422 | 1.73206 | $1.41422 \times 1.73206=2.4495138932$ |
|  |  | $=2.449490772914$ |

## Discussion

If it takes one can of paint to cover a unit square in the coordinate plane, how many cans of paint are needed to paint the region within the curved figure?


## Problem Set

1. Use the following picture to explain why $\frac{15}{12}$ is the same as $1 \frac{1}{4}$.

2. Figures 1 and 2 below show two polygonal regions used to approximate the area of the region inside an ellipse and above the $x$-axis.


a. Which polygonal region has a greater area? Explain your reasoning.
b. Which, if either, of the polygonal regions do you believe is closer in area to the region inside the ellipse and above the $x$-axis?
3. Figures 1 and 2 below show two polygonal regions used to approximate the area of the region inside a parabola and above the $x$-axis.


Figure 1


Figure 2
a. Use the shaded polygonal region in Figure 1 to give a lower estimate of the area $a$ under the curve and above the $x$-axis.
b. Use the shaded polygonal region to give an upper estimate of the area $a$ under the curve and above the $x$-axis.
c. Use (a) and (b) to give an average estimate of the area $a$.
4. Problem 4 is an extension of Problem 3. Using the diagram, draw grid lines to represent each $\frac{1}{2}$ unit.

a. What do the new grid lines divide each unit square into?
b. Use the squares described in part (a) to determine a lower estimate of area $a$ in the diagram.
c. Use the squares described in part (a) to determine an upper estimate of area $a$ in the diagram.
d. Calculate an average estimate of the area under the curve and above the $x$-axis based on your upper and lower estimates in parts (b) and (c).
e. Do you think your average estimate in Problem 4 is more or less precise than your estimate from Problem 3? Explain.

