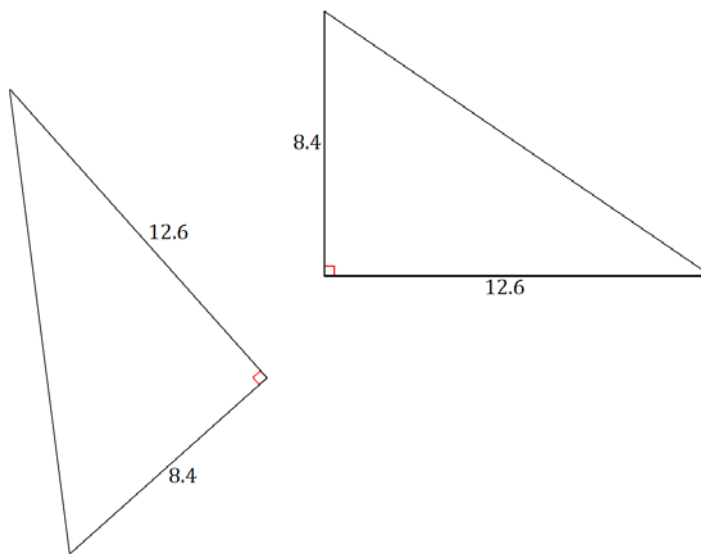


## Lesson 2: Properties of Area

### Classwork

#### Exploratory Challenge/Exercises 1–4

1. Two congruent triangles are shown below.



- a. Calculate the area of each triangle.
- b. Circle the transformations that, if applied to the first triangle, would always result in a new triangle with the same area:

Translation

Rotation

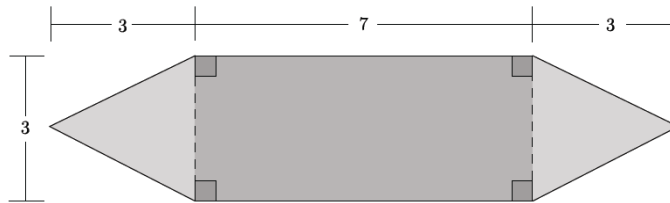
Dilation

Reflection

- c. Explain your answer to part (b).

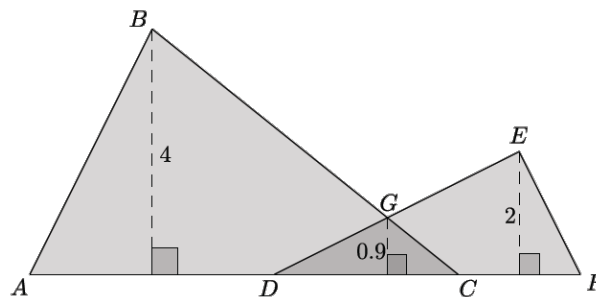
2.

- a. Calculate the area of the shaded figure below.



- b. Explain how you determined the area of the figure.

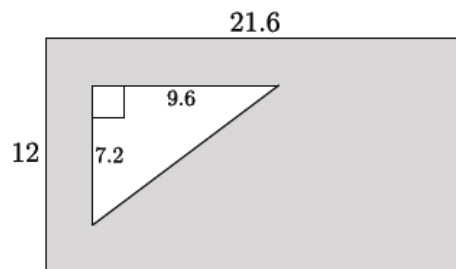
3. Two triangles  $\triangle ABC$  and  $\triangle DEF$  are shown below. The two triangles overlap forming  $\triangle DGC$ .



- a. The base of figure  $ABGEF$  is comprised of segments of the following lengths:  $AD = 4$ ,  $DC = 3$ , and  $CF = 2$ . Calculate the area of the figure  $ABGEF$ .

b. Explain how you determined the area of the figure.

4. A rectangle with dimensions  $21.6 \times 12$  has a right triangle with a base 9.6 and a height of 7.2 cut out of the rectangle.



a. Find the area of the shaded region.

b. Explain how you determined the area of the shaded region.

## Lesson Summary

**SET (DESCRIPTION):** A set is a well-defined collection of objects. These objects are called elements or members of the set.

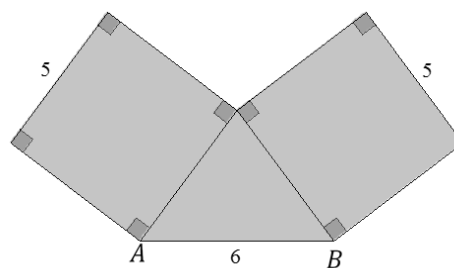
**SUBSET:** A set  $A$  is a *subset* of a set  $B$  if every element of  $A$  is also an element of  $B$ . The notation  $A \subseteq B$  indicates that the set  $A$  is a subset of set  $B$ .

**UNION:** The *union* of  $A$  and  $B$  is the set of all objects that are either elements of  $A$  or of  $B$ , or of both. The union is denoted  $A \cup B$ .

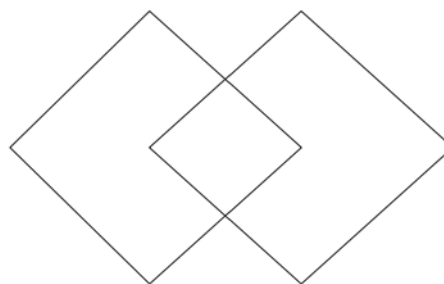
**INTERSECTION:** The *intersection* of  $A$  and  $B$  is the set of all objects that are elements of  $A$  and also elements of  $B$ . The intersection is denoted  $A \cap B$ .

## Problem Set

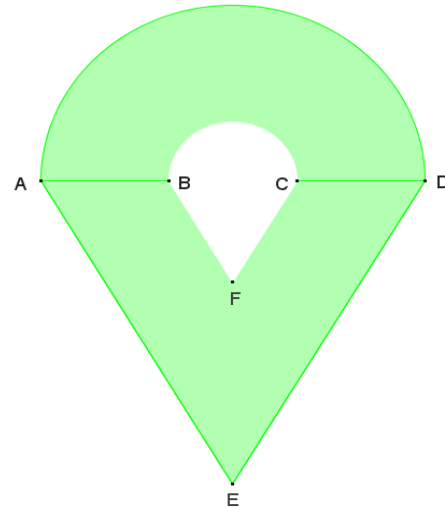
- Two squares with side length 5 meet at a vertex and together with segment  $AB$  form a triangle with base 6 as shown. Find the area of the shaded region.



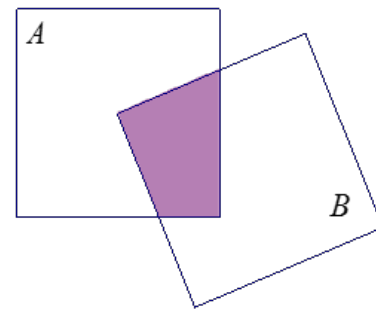
- If two  $2 \times 2$  square regions  $S_1$  and  $S_2$  meet at midpoints of sides as shown, find the area of the square region,  $S_1 \cup S_2$ .



3. The figure shown is composed of a semicircle and a non-overlapping equilateral triangle, and contains a hole that is also composed of a semicircle and a non-overlapping equilateral triangle. If the radius of the larger semicircle is 8, and the radius of the smaller semicircle is  $\frac{1}{3}$  that of the larger semicircle, find the area of the figure.



4. Two square regions  $A$  and  $B$  each have area 8. One vertex of square  $B$  is the center point of square  $A$ . Can you find the area of  $A \cup B$  and  $A \cap B$  without any further information? What are the possible areas?



5. Four congruent right triangles with leg lengths  $a$  and  $b$  and hypotenuse length  $c$  are used to enclose the green region in Figure 1 with a square and then are rearranged inside the square leaving the green region in Figure 2.

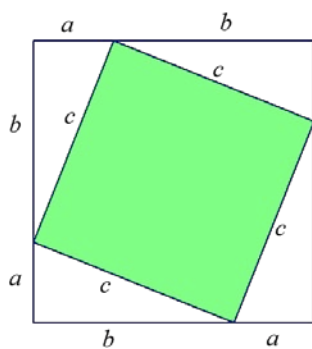


Figure 1

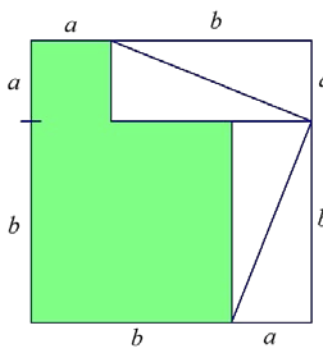


Figure 2

- Use Property 4 to explain why the green region in Figure 1 has the same area as the green region in Figure 2.
- Show that the green region in Figure 1 is a square and compute its area.
- Show that the green region in Figure 2 is the union of two non-overlapping squares and compute its area.
- How does this prove the Pythagorean theorem?