

Lesson 3: Writing Products as Sums and Sums as Products

Classwork

Opening Exercise

Solve the problem using a tape diagram. A sum of money was shared between George and Brian in a ratio of 3: 4. If the sum of money was \$56.00, how much did George get?

Example 1

Represent $3 + 2$ using a tape diagram.

Represent $x + 2$ using a tape diagram.

Draw a rectangular array for $3(3 + 2)$.

Draw an array for $3(x + 2)$.

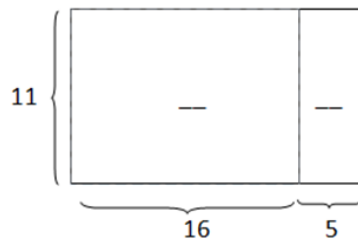
Key Terms

Distributive Property: The distributive property can be written as the identity

$$a(b + c) = ab + ac \text{ for all numbers } a, b, \text{ and } c.$$

Exercise 1

Determine the area of each region using the distributive property.



Example 2

Draw a tape diagram to represent each expression.

a. $(x + y) + (x + y) + (x + y)$

b. $(x + x + x) + (y + y + y)$

c. $3x + 3y$

d. $3(x + y)$

Example 3

Find an equivalent expression by modeling with a rectangular array and applying the distributive property to the expression $5(8x + 3)$.

Exercise 2

For parts (a) and (b), draw an array for each expression and apply the distributive property to expand each expression. Substitute the given numerical values to demonstrate equivalency.

a. $2(x + 1)$, $x = 5$

b. $10(2c + 5)$, $c = 1$

For parts (c) and (d), apply the distributive property. Substitute the given numerical values to demonstrate equivalency.

c. $3(4f - 1), f = 2$

d. $9(-3r - 11), r = 10$

Example 4

Rewrite the expression $(6x + 15) \div 3$ in standard form using the distributive property.

Exercise 3

Rewrite the expressions as a sum.

a. $(2b + 12) \div 2$

b. $(20r - 8) \div 4$

c. $(49g - 7) \div 7$

Example 5

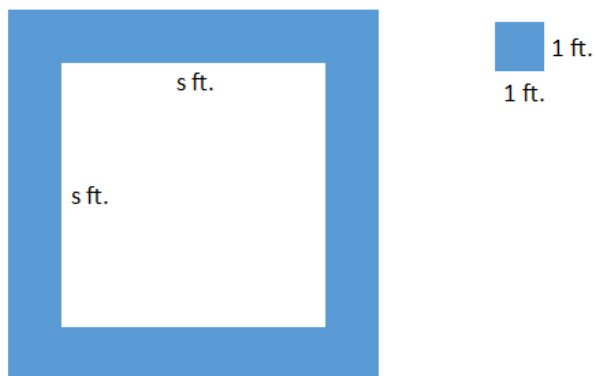
Expand the expression $4(x + y + z)$.

Exercise 4

Expand the expression from a product to a sum by removing grouping symbols using an area model and the repeated use of distributive property: $3(x + 2y + 5z)$.

Example 6

A square fountain area with side length s ft. is bordered by a single row of square tiles as shown. Express the total number of tiles needed in terms of s three different ways.



Problem Set

1.
 - a. Write two equivalent expressions that represent the rectangular array below.
 - b. Verify informally that the two equations are equivalent using substitution.
2. You and your friend made up a basketball shooting game. Every shot made from the free throw line is worth 3 points, and every shot made from the half-court mark is worth 6 points. Write an equation that represents the total amount of points, P , if f represents the number of shots made from the free throw line, and h represents the number of shots made from half-court. Explain the equation in words.
3. Use a rectangular array to write the products in standard form.
 - a. $2(x + 10)$
 - b. $3(4b + 12c + 11)$
4. Use the distributive property to write the products in standard form.

a. $3(2x - 1)$	g. $(40s + 100t) \div 10$
b. $10(b + 4c)$	h. $(48p + 24) \div 6$
c. $9(g - 5h)$	i. $(2b + 12) \div 2$
d. $7(4n - 5m - 2)$	j. $(20r - 8) \div 4$
e. $a(b + c + 1)$	k. $(49g - 7) \div 7$
f. $(8j - 3l + 9)6$	l. $(14g + 22h) \div \frac{1}{2}$
5. Write the expression in standard form by expanding and collecting like terms.
 - a. $4(8m - 7n) + 6(3n - 4m)$
 - b. $9(r - s) + 5(2r - 2s)$
 - c. $12(1 - 3g) + 8(g + f)$