Name $\qquad$ Date $\qquad$

## Lesson 1: Chance Experiments

## Exit Ticket

Decide where each of the following events would be located on the scale below. Place the letter for each event on the appropriate place on the probability scale.

## PROBABILITY SCALE



The numbers from 1 to 10 are written on small pieces of paper and placed in a bag. A piece of paper will be drawn from the bag.
A. A piece of paper with a 5 is drawn from the bag.
B. A piece of paper with an even number is drawn.
C. A piece of paper with a 12 is drawn.
D. A piece of paper with a number other than 1 is drawn.
E. A piece of paper with a number divisible by 5 is drawn.

Name $\qquad$ Date $\qquad$

## Lesson 2: Estimating Probabilities by Collecting Data

## Exit Ticket

In the following problems, round all of your decimal answers to 3 decimal places. Round all of your percents to the nearest tenth of a percent.

A student randomly selected crayons from a large bag of crayons. The table below shows the number of each color crayon in a bag. Now, suppose the student were to randomly select one crayon from the bag.

| Color | Number |
| :---: | :---: |
| Brown | 10 |
| Blue | 5 |
| Yellow | 3 |
| Green | 3 |
| Orange | 3 |
| Red | 6 |

1. What is the estimate for the probability of selecting a blue crayon from the bag? Express your answer as a fraction, decimal, or percent.
2. What is the estimate for the probability of selecting a brown crayon from the bag?
3. What is the estimate for the probability of selecting a red crayon or a yellow crayon from the bag?
4. What is the estimate for the probability of selecting a pink crayon from the bag?
5. Which color is most likely to be selected?
6. If there are 300 crayons in the bag, how many will be red? Justify your answer.
$\qquad$

## Lesson 3: Chance Experiments with Equally Likely Outcomes

## Exit Ticket

The numbers from 1-10 are written on note cards and placed in a bag. One card will be drawn from the bag at random.

1. List the sample space for this experiment.
2. Are the events selecting an even number and selecting an odd number equally likely? Explain your answer.
3. Are the events selecting a number divisible by 3 and selecting a number divisible by 5 equally likely? Explain your answer.
$\qquad$

# Lesson 4: Calculating Probabilities for Chance Experiments with Equally Likely Outcomes 

## Exit Ticket

An experiment consists of randomly drawing a cube from a bag containing three red and two blue cubes.

1. What is the sample space of this experiment?
2. List the probability of each outcome in the sample space.
3. Is the probability of selecting a red cube equal to the probability of selecting a blue cube? Explain.
$\qquad$ Date $\qquad$

## Lesson 5: Chance Experiments with Outcomes That Are Not

## Equally Likely

## Exit Ticket

Carol is sitting on the bus on the way home from school and is thinking about the fact that she has three homework assignments to do tonight. The table below shows her estimated probabilities of completing $0,1,2$, or all 3 of the assignments.

| Number of Homework Assignments Completed | 0 | 1 | 2 | 3 |
| :--- | :---: | :---: | :---: | :---: |
| Probability | $\frac{1}{6}$ | $\frac{2}{9}$ | $\frac{5}{18}$ | $\frac{1}{3}$ |

1. Writing your answers as fractions in lowest terms, find the probability that Carol completes
a. Exactly one assignment.
b. More than one assignment.
c. At least one assignment.
2. Find the probability that the number of homework assignments Carol completes is not exactly 2.
3. Carol has a bag containing 3 red chips, 10 blue chips, and 7 green chips. Estimate the probability (as a fraction or decimal) of Carol reaching into her bag and pulling out a green chip.
$\qquad$

## Lesson 6: Using Tree Diagrams to Represent a Sample Space and

 to Calculate Probabilities
## Exit Ticket

In a laboratory experiment, two mice will be placed in a simple maze with one decision point where a mouse can turn either left ( $L$ ) or right ( $R$ ). When the first mouse arrives at the decision point, the direction it chooses is recorded. Then, the process is repeated for the second mouse.

1. Draw a tree diagram where the first stage represents the decision made by the first mouse, and the second stage represents the decision made by the second mouse. Determine all four possible decision outcomes for the two mice.
2. If the probability of turning left is 0.5 , and the probability of turning right is 0.5 for each mouse, what is the probability that only one of the two mice will turn left?
3. If the researchers add food in the simple maze such that the probability of each mouse turning left is now 0.7 , what is the probability that only one of the two mice will turn left?

## Lesson 7: Calculating Probabilities of Compound Events

## Exit Ticket

In a laboratory experiment, three mice will be placed in a simple maze that has just one decision point where a mouse can turn either left ( $L$ ) or right ( $R$ ). When the first mouse arrives at the decision point, the direction he chooses is recorded. The same is done for the second and the third mice.

1. Draw a tree diagram where the first stage represents the decision made by the first mouse, and the second stage represents the decision made by the second mouse, and so on. Determine all eight possible outcomes of the decisions for the three mice.
2. Use the tree diagram from Question 1 to help answer the following question. If, for each mouse, the probability of turning left is 0.5 and the probability of turning right is 0.5 , what is the probability that only one of the three mice will turn left?
3. If the researchers conducting the experiment add food in the simple maze such that the probability of each mouse turning left is now 0.7 , what is the probability that only one of the three mice will turn left? To answer the question, use the tree diagram from Question 1.
$\qquad$
$\qquad$

## Lesson 8: The Difference Between Theoretical Probabilities and Estimated Probabilities

## Exit Ticket

1. Which of the following graphs would NOT represent the relative frequencies of heads when tossing 1 penny? Explain your answer.

Graph A


Graph B

2. Jerry indicated that after tossing a penny 30 times, the relative frequency of heads was 0.47 (to the nearest hundredth). He indicated that after 31 times, the relative frequency of heads was 0.55 . Are Jerry's summaries correct? Why or why not?
3. Jerry observed 5 heads in 100 tosses of his coin. Do you think this was a fair coin? Why or why not?
$\qquad$

# Lesson 10: Conducting a Simulation to Estimate the Probability of 

## an Event

## Exit Ticket

1. Nathan is your school's star soccer player. When he takes a shot on goal he typically scores half of the time. Suppose that he takes six shots in a game. To estimate the probability of the number of goals Nathan makes, use simulation with a number cube. One roll of a number cube represents one shot.
a. Specify what outcome of a number cube you want to represent a goal scored by Nathan in one shot.
b. For this problem, what represents a trial of taking six shots?
c. Perform and list the results of ten trials of this simulation.
d. Identify the number of goals Nathan made in each of the ten trials you did in part (c).
e. Based on your ten trials, what is your estimate of the probability that Nathan scores three goals if he takes six shots in a game?
2. Suppose that Pat scores $40 \%$ of the shots he takes in a soccer game. If he takes six shots in a game, what would one simulated trial look like using a number cube in your simulation?

Name $\qquad$ Date $\qquad$

# Lesson 11: Conducting a Simulation to Estimate the Probability of 

## an Event

## Exit Ticket

Liang wants to form a chess club. His principal says that he can do that if Liang can find six players, including him. How would you conduct a simulated model that estimates the probability that Liang will find at least five other players to join the club if he asks eight players who have a $70 \%$ chance of agreeing to join the club? Suggest a simulation model for Liang by describing how you would do the following parts.
a. Specify the device you want to use to simulate one person being asked.
b. What outcome(s) of the device would represent the person agreeing to be a member?
c. What constitutes a trial using your device in this problem?
d. What constitutes a success using your device in this problem?
e. Based on 50 trials, using the method you have suggested, how would you calculate the estimate for the probability that Liang will be able to form a chess club?
$\qquad$

## Lesson 12: Applying Probability to Make Informed Decisions

## Exit Ticket

There are four pieces of bubble gum left in a quarter machine. Two are red and two are yellow. Chandra puts two quarters in the machine. One piece is for her and one is for her friend, Kay. If the two pieces are the same color, she is happy because they will not have to decide who gets what color. Chandra claims that they are equally likely to get the same color because the colors are either the same or they are different. Check her claim by doing a simulation.
a. Name a device that can be used to simulate getting a piece of bubble gum. Specify what outcome of the device represents a red piece and what outcome represents yellow.
b. Define what a trial is for your simulation.
c. Define what constitutes a success in a trial of your simulation.
d. Perform and list 50 simulated trials. Based on your results, is Chandra's equally likely model correct?

Name $\qquad$ Date $\qquad$

Round all decimal answers to the nearest hundredth.

1. Each student in a class of 38 students was asked to report how many siblings (brothers and sisters) he or she has. The data are summarized in the table below.

| Number of <br> Siblings | 0 | 1 | 2 | 3 | 4 | 5 | 6 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Count | 8 | 13 | 12 | 3 | 1 | 0 | 1 |

a. Based on the data, estimate the probability that a randomly selected student from this class is an only child.
b. Based on the data, estimate the probability that a randomly selected student from this class has three or more siblings.
c. Consider the following probability distribution for the number of siblings:

| Number of <br> Siblings | 0 | 1 | 2 | 3 | 4 | 5 | 6 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Probability | 0.15 | 0.35 | 0.30 | 0.10 | 0.05 | 0.03 | 0.02 |

Explain how you could use simulation to estimate the probability that you will need to ask at least five students the question, "Are you an only child?" if each is an only child before you find the first one that is an only child.
2. A cell phone company wants to predict the probability of a seventh grader in your city, City A, owning a cell phone. Records from another city, City B, indicate that 201 of 1,000 seventh graders own a cell phone.
a. Assuming the probability of a seventh grader owning a cell phone is similar for the two cities, estimate the probability that a randomly selected seventh grader from City A owns a cell phone.
b. The company estimates the probability that a randomly selected seventh-grade male owns a cell phone is 0.25 . Does this imply that the probability that a randomly selected seventh-grade female owns a cell phone is 0.75 ? Explain.
c. According to the data, which of the following is more likely?

- a seventh-grade male owning a cell phone
- a seventh grader owning a cell phone

Explain your choice.

Suppose the cell phone company sells three different plans to its customers:

- Pay-as-you-go: Customer is charged per minute for each call.
- Unlimited minutes: Customer pays a flat fee per month and can make unlimited calls with no additional charges.
- Basic plan: Customer not charged per minute unless the customer exceeds 500 minutes in the month; then, the customer is charged per minute for the extra minutes.

Consider the chance experiment of selecting a customer at random and recording which plan they purchased.
d. What outcomes are in the sample space for this chance experiment?
e. The company wants to assign probabilities to these three plans. Explain what is wrong with each of the following probability assignments.

Case 1: Probability of pay-as-you-go $=0.40$, probability of unlimited minutes $=0.40$, and probability of basic plan $=0.30$.

Case 2: Probability of pay-as-you-go $=0.40$, probability of unlimited minutes $=0.70$, and probability of basic plan $=-0.10$.

Now consider the chance experiment of randomly selecting a cell phone customer and recording both the cell phone plan for that customer and whether or not the customer exceeded 500 minutes last month.
f. One possible outcome of this chance experiment is (pay-as-you-go, over 500). What are the other possible outcomes in this sample space?
g. Assuming the outcomes of this chance experiment are equally likely, what is the probability that the selected cell phone customer had a basic plan and did not exceed 500 minutes last month?
h. Suppose the company randomly selects 500 of its customers and finds that 140 of these customers purchased the basic plan and did not exceed 500 minutes. Would this cause you to question the claim that the outcomes of the chance experiment described in part (g) are equally likely? Explain why or why not.
3. In the game of Darts, players throw darts at a circle divided into 20 wedges. In one variation of the game, the score for a throw is equal to the wedge number that the dart hits. So, if the dart hits anywhere in the 20 wedge, you earn 20 points for that throw.

a. If you are equally likely to land in any wedge, what is the probability you will score 20 points?
b. If you are equally likely to land in any wedge, what is the probability you will land in the upper right and score $20,1,18,4,13$, or 6 points?
c. Below are the results of 100 throws for one player. Does this player appear to have a tendency to land in the upper right more often than we would expect if the player was equally likely to land in any wedge?

| Points | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 10 | 11 | 12 | 13 | 14 | 15 | 16 | 17 | 18 | 19 | 20 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Count | 7 | 9 | 2 | 6 | 6 | 3 | 5 | 2 | 4 | 7 | 2 | 6 | 4 | 6 | 5 | 7 | 4 | 6 | 5 | 4 |

$\qquad$

## Lesson 13: Populations, Samples, and Generalizing from a Sample to a Population

## Exit Ticket

What is the difference between a population characteristic and a sample statistic? Give an example to support your answer. Clearly identify the population and sample in your example.

Name $\qquad$ Date $\qquad$

## Lesson 14: Selecting a Sample

Exit Ticket

Write down three things you learned about taking a sample from the work we have done today.

## Handout

## \1 \Casey at the Bat

The Outlook wasn't brilliant for the Mudville nine that day: The score stood four to two, \2 $\backslash$ with but one inning more to play. And then when Cooney died at first, and Barrows did the same, $\mathrm{A} \backslash \mathbf{3} \backslash$ sickly silence fell upon the patrons of the game.

A straggling few got up to go in deep despair. The $\backslash 4 \backslash$ rest Clung to that hope which springs eternal in the human breast; They thought, if only Casey could get but $\backslash \mathbf{5}$ \a whack at that-We'd put up even money, now, with Casey at the bat.

But Flynn preceded Casey, as $\backslash \mathbf{6} \backslash$ did also Jimmy Blake, And the former was a lulu and the latter was a cake; So upon that stricken \7\ multitude grim melancholy sat, For there seemed but little chance of Casey's getting to the bat.

But Flynn let drive \8\a single, to the wonderment of all, And Blake, the much despised, tore the cover off the ball; And when $\backslash 9 \backslash$ the dust had lifted, and the men saw what had occurred, There was Jimmy safe at second and Flynn a $\backslash \mathbf{1 0}$ \hugging third.

Then from five thousand throats and more there rose a lusty yell; It rumbled through the valley, it \11\ rattled in the dell; It knocked upon the mountain and recoiled upon the flat, For Casey, mighty Casey, was advancing \12\to the bat.

There was ease in Casey's manner as he stepped into his place; There was pride in Casey's $\backslash \mathbf{1 3} \backslash$ bearing and a smile on Casey's face. And when, responding to the cheers, he lightly doffed his hat, No stranger $\backslash \mathbf{1 4}$ \in the crowd could doubt 'twas Casey at the bat.

Ten thousand eyes were on him as he rubbed his $\backslash \mathbf{1 5}$ \hands with dirt; Five thousand tongues applauded when he wiped them on his shirt. Then while the writhing pitcher ground $\backslash \mathbf{1 6}$ \the ball into his hip, Defiance gleamed in Casey's eye, a sneer curled Casey’s lip.

And now the leather covered $\backslash \mathbf{1 7} \backslash$ sphere came hurtling through the air, And Casey stood a-watching it in haughty grandeur there. Close by the sturdy batsman $\backslash \mathbf{1 8} \backslash$ the ball unheeded sped—"That ain't my style," said Casey. "Strike one," the umpire said.

From the benches, black with $\backslash \mathbf{1 9}$ \people, there went up a muffled roar, Like the beating of the storm waves on a stern and distant shore. \20\"Kill him! Kill the umpire!" shouted someone on the stand; And it's likely they'd a-killed him had not Casey raised $\backslash \mathbf{2 1} \backslash$ his hand.

With a smile of Christian charity great Casey's visage shone; He stilled the rising tumult; he bade the \22\} game go on; He signaled to the pitcher, and once more the spheroid flew; But Casey still ignored it, and $\backslash \mathbf{2 3} \backslash$ the umpire said, "Strike two."
"Fraud!" cried the maddened thousands, and echo answered fraud; But one scornful look from Casey $\backslash \mathbf{2 4}$ \and the audience was awed. They saw his face grow stern and cold, they saw his muscles strain, And they $\backslash \mathbf{2 5} \backslash$ knew that Casey wouldn't let that ball go by again.

The sneer is gone from Casey's lip, his teeth are $\backslash \mathbf{2 6}$ \clenched in hate; He pounds with cruel violence his bat upon the plate. And now the pitcher holds the ball, $\backslash \mathbf{2 7} \backslash$ and now he lets it go, And now the air is shattered by the force of Casey's blow.

Oh, somewhere $\backslash \mathbf{2 8} \backslash$ in this favored land the sun is shining bright; The band is playing somewhere, and somewhere hearts are light, And $\backslash \mathbf{2 9}$ \somewhere men are laughing, and somewhere children shout; But there is no joy in Mudville -mighty Casey has struck out.
by Ernest Lawrence Thayer
$\qquad$ Date $\qquad$

## Lesson 15: Random Sampling

## Exit Ticket

Identify each as true or false. Explain your reasoning in each case.

1. The values of a sample statistic for different random samples of the same size from the same population will be the same.
2. Random samples from the same population will vary from sample to sample.
3. If a random sample is chosen from a population that has a large cluster of points at the maximum, the sample is likely to have at least one element near the maximum.

## 100 Grocery Items (2013 prices)

| T-bone steaks \$6.99 (1 lb.) | Porterhouse steaks \$7.29 (1 lb.) | Pasta sauce \$2.19 (16 oz.) | Ice cream cups \$7.29 (6 cups) |
| :---: | :---: | :---: | :---: |
| Hot dog buns \$0.88 (6 buns) | Baking chips \$2.99 (12 oz.) | $\begin{aligned} & \text { Cheese chips } \\ & \$ 2.09 \text { (12 oz.) } \end{aligned}$ | $\begin{gathered} \text { Cookies } \\ \text { \$1.77 (15 oz.) } \end{gathered}$ |
| Kidney beans \$0.77 (15 oz.) | Box of oatmeal \$1.77 (18 oz.) | $\begin{gathered} \text { Soup } \\ \$ 0.77 \text { (14 oz.) } \end{gathered}$ | Chicken breasts \$7.77 (1.5 lb.) |
| Pancake syrup \$2.99 (28 oz.) | Cranberry juice \$2.77 (64 oz.) | Asparagus \$3.29 (1 lb.) | Seedless cucumbers \$1.29 (1 ct.) |
| $\begin{gathered} \text { Avocado } \\ \$ 1.30 \text { (1 ct.) } \end{gathered}$ | Sliced pineapple $\$ 2.99$ | Box of tea \$4.29 (16 tea bags) | Cream cheese \$2.77 (16 oz.) |
| $\begin{gathered} \text { Italian roll } \\ \$ 1.39 \text { (1 roll) } \end{gathered}$ | Turkey breast \$4.99 (1 lb.) | $\begin{gathered} \text { Meatballs } \\ \$ 5.79 \text { (26 oz.) } \end{gathered}$ | $\begin{gathered} \text { Chili } \\ \$ 1.35 \text { (15 oz.) } \end{gathered}$ |
| Peanut butter \$1.63 (12 oz.) | $\begin{aligned} & \text { Green beans } \\ & \$ 0.99 \text { (1 lb.) } \end{aligned}$ | Apples \$1.99 (1 lb.) | Mushrooms \$0.69 (8 oz.) |
| Brown sugar \$1.29 (32 oz.) | Confectioners' sugar \$1.39 (32 oz.) | $\begin{gathered} \text { Zucchini } \\ \$ 0.79(1 \mathrm{lb} .) \end{gathered}$ | Yellow onions $\$ 0.99 \text { (1 lb.) }$ |
| Green peppers \$0.99 (1 ct.) | Mozzarella cheese \$2.69 (8 oz.) | Frozen chicken \$6.49 (48 oz.) | $\begin{gathered} \text { Olive oil } \\ \$ 2.99 \text { (17 oz.) } \end{gathered}$ |
| Dark chocolate \$2.99 (9 oz.) | Cocoa mix \$3.33 (1 package) | $\begin{gathered} \text { Margarine } \\ \$ 1.48 \text { (16 oz.) } \end{gathered}$ | Mac and cheese \$0.66 (6 oz. box) |
| Birthday cake $\$ 9.49 \text { (7 in.) }$ | $\begin{gathered} \text { Crab legs } \\ \$ 19.99 \text { (1 lb.) } \end{gathered}$ | $\begin{gathered} \text { Sushi rolls } \\ \$ 12.99 \text { (20 ct.) } \end{gathered}$ | $\begin{gathered} \text { Prime rib } \\ \$ 19.99 \text { (4 lb.) } \end{gathered}$ |
| Cooked shrimp \$12.99 (32 oz.) | $\begin{gathered} \text { Ice cream } \\ \$ 4.49 \text { (1 qt.) } \end{gathered}$ | Pork chops \$1.79 (1 lb.) | $\begin{gathered} \text { Bananas } \\ \$ 0.44(1 \mathrm{lb} .) \end{gathered}$ |
| Chocolate milk \$2.99 (1 gal.) | Beeffranks $\$ 3.35(1 \mathrm{lb} .)$ | Sliced bacon \$5.49 (1 lb.) | Fish fillets $\$ 6.29 \text { (1 lb.) }$ |


| $\begin{gathered} \text { Pears } \\ \$ 1.29(1 \mathrm{lb} .) \end{gathered}$ | Tangerines \$3.99 (3 lb.) | Orange juice \$2.98 (59 oz.) | Cherry pie \$4.44 (8 in.) |
| :---: | :---: | :---: | :---: |
| Grapes \$1.28 (1 lb.) | $\begin{gathered} \text { Peaches } \\ \$ 1.28 \text { (1 lb.) } \end{gathered}$ | Melon \$1.69 (1 melon) | $\begin{aligned} & \text { Tomatoes } \\ & \$ 1.49 \text { (1 lb.) } \end{aligned}$ |
| Shredded cheese \$1.88 (12 oz.) | $\begin{gathered} \text { Soda } \\ \$ 0.88(1 \mathrm{can}) \end{gathered}$ | Roast beef \$6.49 (1 lb.) | Coffee $\$ 6.49$ (1 lb.) |
| Feta cheese $\$ 4.99$ (1 lb.) | Pickles <br> \$1.69 (12 oz. jar) | Loaf of rye bread \$2.19 | $\begin{gathered} \text { Crackers } \\ \$ 2.69 \text { (7.9 oz.) } \end{gathered}$ |
| Purified water \$3.47 (35 pk.) | $\begin{gathered} \text { BBQ sauce } \\ \$ 2.19 \text { (24 oz.) } \end{gathered}$ | $\begin{gathered} \text { Ketchup } \\ \$ 2.29 \text { (34 oz.) } \end{gathered}$ | $\begin{gathered} \text { Chili sauce } \\ \$ 1.77 \text { (12 oz.) } \end{gathered}$ |
| Sugar \$1.77 (5 lb.) | Flour \$2.11 (4 lb.) | Breakfast cereal \$2.79 (9 oz.) | Cane sugar \$2.39 (4 lb.) |
| Cheese sticks \$1.25 (10 oz.) | Cheese spread \$2.49 (45 oz.) | Coffee creamer \$2.99 (12 oz.) | $\begin{gathered} \text { Candy bars } \\ \$ 7.77 \text { (40 oz.) } \end{gathered}$ |
| Pudding mix \$0.98 (6 oz.) | Fruit drink \$1.11 (24 oz.) | $\begin{gathered} \text { Biscuit mix } \\ \$ 0.89(4 \mathrm{oz} .) \end{gathered}$ | $\begin{gathered} \text { Sausages } \\ \$ 2.38 \text { (13 oz.) } \end{gathered}$ |
| Ground beef \$4.49 (1 lb.) | $\begin{gathered} \text { Apple juice } \\ \text { \$1.48 (64 oz.) } \end{gathered}$ | Ice cream sandwich \$1.98 (12 ct.) | Cottage cheese \$1.98 (24 oz.) |
| Frozen vegetables \$0.88 (10 oz.) | English muffins $\$ 1.68$ (6 ct.) | String cheese \$6.09 (24 oz.) | $\begin{gathered} \text { Baby greens } \\ \$ 2.98 \text { (10 oz.) } \end{gathered}$ |
| Caramel apples \$3.11 (1 ct.) | Pumpkin mix $\$ 3.50$ (1 lb.) | Chicken salad \$0.98 (2 oz.) | Whole wheat bread \$1.55 (1 loaf) |
| $\begin{gathered} \text { Tuna } \\ \$ 0.98(2.5 \mathrm{oz} .) \end{gathered}$ | Nutrition bar \$2.19 (1 bar) | $\begin{aligned} & \text { Potato chips } \\ & \$ 2.39 \text { (12 oz.) } \end{aligned}$ | 2\% milk \$3.13 (1 gal.) |

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## Lesson 16: Methods for Selecting a Random Sample

## Exit Ticket

1. Name two things to consider when you are planning how to select a random sample.
2. Consider a population consisting of the 200 seventh graders at a particular middle school. Describe how you might select a random sample of 20 students from a list of the students in this population.

Name $\qquad$ Date $\qquad$

## Lesson 17: Sampling Variability

## Exit Ticket

Suppose that you want to estimate the mean time per evening students at your school spend doing homework. You will do this using a random sample of 30 students.

1. Suppose that you have a list of all the students at your school. The students are numbered $1,2,3, \ldots$. One way to select the random sample of students is to use the random digit table from today's class, taking three digits at a time. If you start at the third digit of row 9, what is the number of the first student you would include in your sample?
2. Suppose that you have now selected your random sample and that you have asked the students how long they spend doing homework each evening. How will you use these results to estimate the mean time spent doing homework for all students?
3. Explain what is meant by sampling variability in this context.

## Lesson 18: Sampling Variability and the Effect of Sample Size

## Exit Ticket

Suppose that you wanted to estimate the mean time per evening spent doing homework for students at your school. You decide to do this by taking a random sample of students from your school. You will calculate the mean time spent doing homework for your sample. You will then use your sample mean as an estimate of the population mean.

1. The sample mean has sampling variability. Explain what this means.
2. When you are using a sample statistic to estimate a population characteristic, do you want the sampling variability of the sample statistic to be large or small? Explain why.
3. Think about your estimate of the mean time spent doing homework for students at your school. Given a choice of using a sample of size 20 or a sample of size 40, which should you choose? Explain your answer.

Name $\qquad$ Date $\qquad$

## Lesson 19: Understanding Variability When Estimating a

 Population Proportion
## Exit Ticket

A group of seventh graders took repeated samples of size 20 from a bag of colored cubes. The dot plot below shows the sampling distribution of the sample proportion of blue cubes in the bag.


1. Describe the shape of the distribution.
2. Describe the variability of the distribution.
3. Predict how the dot plot would look differently if the sample sizes had been 40 instead of 20 .

Name $\qquad$ Date $\qquad$

## Lesson 20: Estimating a Population Proportion

## Exit Ticket

Thirty seventh graders each took a random sample of 10 middle school students and asked each student whether or not they like pop music. Then, they calculated the proportion of students who like pop music for each sample. The dot plot below shows the distribution of the sample proportions.

## Dot Plot of Sample Proportions for $\mathbf{n = 1 0}$



1. There are three dots above 0.2 . What does each dot represent in terms of this scenario?
2. Based on the dot plot, do you think the proportion of the middle school students at this school who like pop music is 0.6 ? Explain why or why not.

| Row |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 1 | 6 | 6 | 7 | 2 | 8 | 0 | 0 | 8 | 4 | 0 | 0 | 4 | 6 | 0 | 3 | 2 | 2 | 4 | 6 | 8 |
| 2 | 8 | 0 | 3 | 1 | 1 | 1 | 1 | 2 | 7 | 0 | 1 | 9 | 1 | 2 | 7 | 1 | 3 | 3 | 5 | 3 |
| 3 | 5 | 3 | 5 | 7 | 3 | 6 | 3 | 1 | 7 | 2 | 5 | 5 | 1 | 4 | 7 | 1 | 6 | 5 | 6 | 5 |
| 4 | 9 | 1 | 1 | 9 | 2 | 8 | 3 | 0 | 3 | 6 | 7 | 7 | 4 | 7 | 5 | 9 | 8 | 1 | 8 | 3 |
| 5 | 9 | 0 | 2 | 9 | 9 | 7 | 4 | 6 | 3 | 6 | 6 | 3 | 7 | 4 | 2 | 7 | 0 | 0 | 1 | 9 |
| 6 | 8 | 1 | 4 | 6 | 4 | 6 | 8 | 2 | 8 | 9 | 5 | 5 | 2 | 9 | 6 | 2 | 5 | 3 | 0 | 3 |
| 7 | 4 | 1 | 1 | 9 | 7 | 0 | 7 | 2 | 9 | 0 | 9 | 7 | 0 | 4 | 6 | 2 | 3 | 1 | 0 | 9 |
| 8 | 9 | 9 | 2 | 7 | 1 | 3 | 2 | 9 | 0 | 3 | 9 | 0 | 7 | 5 | 6 | 7 | 1 | 7 | 8 | 7 |
| 9 | 3 | 4 | 2 | 2 | 9 | 1 | 9 | 0 | 7 | 8 | 1 | 6 | 2 | 5 | 3 | 9 | 0 | 9 | 1 | 0 |
| 10 | 2 | 7 | 3 | 9 | 5 | 9 | 9 | 3 | 2 | 9 | 3 | 9 | 1 | 9 | 0 | 5 | 5 | 1 | 4 | 2 |
| 11 | 0 | 2 | 5 | 4 | 0 | 8 | 1 | 7 | 0 | 7 | 1 | 3 | 0 | 4 | 3 | 0 | 6 | 4 | 4 | 4 |
| 12 | 8 | 6 | 0 | 5 | 4 | 8 | 8 | 2 | 7 | 7 | 0 | 1 | 0 | 1 | 7 | 1 | 3 | 5 | 3 | 4 |
| 13 | 4 | 2 | 6 | 4 | 5 | 2 | 4 | 2 | 6 | 1 | 7 | 5 | 6 | 6 | 4 | 0 | 8 | 4 | 1 | 2 |
| 14 | 4 | 4 | 9 | 8 | 7 | 3 | 4 | 3 | 8 | 2 | 9 | 1 | 5 | 3 | 5 | 9 | 8 | 9 | 2 | 9 |
| 15 | 6 | 4 | 8 | 0 | 0 | 0 | 4 | 2 | 3 | 8 | 1 | 8 | 4 | 0 | 9 | 5 | 0 | 9 | 0 | 4 |
| 16 | 3 | 2 | 3 | 8 | 4 | 8 | 8 | 6 | 2 | 9 | 1 | 0 | 1 | 9 | 9 | 3 | 0 | 7 | 3 | 5 |
| 17 | 6 | 6 | 7 | 2 | 8 | 0 | 0 | 8 | 4 | 0 | 0 | 4 | 6 | 0 | 3 | 2 | 2 | 4 | 6 | 8 |
| 18 | 8 | 0 | 3 | 1 | 1 | 1 | 1 | 2 | 7 | 0 | 1 | 9 | 1 | 2 | 7 | 1 | 3 | 3 | 5 | 3 |
| 19 | 5 | 3 | 5 | 7 | 3 | 6 | 3 | 1 | 7 | 2 | 5 | 5 | 1 | 4 | 7 | 1 | 6 | 5 | 6 | 5 |
| 20 | 9 | 1 | 1 | 9 | 2 | 8 | 3 | 0 | 3 | 6 | 7 | 7 | 4 | 7 | 5 | 9 | 8 | 1 | 8 | 3 |
| 21 | 9 | 0 | 2 | 9 | 9 | 7 | 4 | 6 | 3 | 6 | 6 | 3 | 7 | 4 | 2 | 7 | 0 | 0 | 1 | 9 |
| 22 | 8 | 1 | 4 | 6 | 4 | 6 | 8 | 2 | 8 | 9 | 5 | 5 | 2 | 9 | 6 | 2 | 5 | 3 | 0 | 3 |
| 23 | 4 | 1 | 1 | 9 | 7 | 0 | 7 | 2 | 9 | 0 | 9 | 7 | 0 | 4 | 6 | 2 | 3 | 1 | 0 | 9 |
| 24 | 9 | 9 | 2 | 7 | 1 | 3 | 2 | 9 | 0 | 3 | 9 | 0 | 7 | 5 | 6 | 7 | 1 | 7 | 8 | 7 |
| 25 | 3 | 4 | 2 | 2 | 9 | 1 | 9 | 0 | 7 | 8 | 1 | 6 | 2 | 5 | 3 | 9 | 0 | 9 | 1 | 0 |
| 26 | 2 | 7 | 3 | 9 | 5 | 9 | 9 | 3 | 2 | 9 | 3 | 9 | 1 | 9 | 0 | 5 | 5 | 1 | 4 | 2 |
| 27 | 0 | 2 | 5 | 4 | 0 | 8 | 1 | 7 | 0 | 7 | 1 | 3 | 0 | 4 | 3 | 0 | 6 | 4 | 4 | 4 |
| 28 | 8 | 6 | 0 | 5 | 4 | 8 | 8 | 2 | 7 | 7 | 0 | 1 | 0 | 1 | 7 | 1 | 3 | 5 | 3 | 4 |
| 29 | 4 | 2 | 6 | 4 | 5 | 2 | 4 | 2 | 6 | 1 | 7 | 5 | 6 | 6 | 4 | 0 | 8 | 4 | 1 | 2 |
| 30 | 4 | 4 | 9 | 8 | 7 | 3 | 4 | 3 | 8 | 2 | 9 | 1 | 5 | 3 | 5 | 9 | 8 | 9 | 2 | 9 |
| 31 | 6 | 4 | 8 | 0 | 0 | 0 | 4 | 2 | 3 | 8 | 1 | 8 | 4 | 0 | 9 | 5 | 0 | 9 | 0 | 4 |
| 32 | 3 | 2 | 3 | 8 | 4 | 8 | 8 | 6 | 2 | 9 | 1 | 0 | 1 | 9 | 9 | 3 | 0 | 7 | 3 | 5 |
| 33 | 6 | 6 | 7 | 2 | 8 | 0 | 0 | 8 | 4 | 0 | 0 | 4 | 6 | 0 | 3 | 2 | 2 | 4 | 6 | 8 |
| 34 | 8 | 0 | 3 | 1 | 1 | 1 | 1 | 2 | 7 | 0 | 1 | 9 | 1 | 2 | 7 | 1 | 3 | 3 | 5 | 3 |
| 35 | 5 | 3 | 5 | 7 | 3 | 6 | 3 | 1 | 7 | 2 | 5 | 5 | 1 | 4 | 7 | 1 | 6 | 5 | 6 | 5 |
| 36 | 9 | 1 | 1 | 9 | 2 | 8 | 3 | 0 | 3 | 6 | 7 | 7 | 4 | 7 | 5 | 9 | 8 | 1 | 8 | 3 |
| 37 | 9 | 0 | 2 | 9 | 9 | 7 | 4 | 6 | 3 | 6 | 6 | 3 | 7 | 4 | 2 | 7 | 0 | 0 | 1 | 9 |
| 38 | 8 | 1 | 4 | 6 | 4 | 6 | 8 | 2 | 8 | 9 | 5 | 5 | 2 | 9 | 6 | 2 | 5 | 3 | 0 | 3 |
| 39 | 4 | 1 | 1 | 9 | 7 | 0 | 7 | 2 | 9 | 0 | 9 | 7 | 0 | 4 | 6 | 2 | 3 | 1 | 0 | 9 |
| 40 | 9 | 9 | 2 | 7 | 1 | 3 | 2 | 9 | 0 | 3 | 9 | 0 | 7 | 5 | 6 | 7 | 1 | 7 | 8 | 7 |


| ID | Travel to School | Favorite Season | Allergies | Favorite School Subject | Favorite Music | Superpower |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 1 | Car | Spring | Yes | English | Pop | Freeze time |
| 2 | Car | Summer | Yes | Music | Pop | Telepathy |
| 3 | Car | Summer | No | Science | Pop | Fly |
| 4 | Walk | Fall | No | Computers and technology | Pop | Invisibility |
| 5 | Car | Summer | No | Art | Country | Telepathy |
| 6 | Car | Summer | No | Physical education | Rap/Hip hop | Freeze time |
| 7 | Car | Spring | No | Physical education | Pop | Telepathy |
| 8 | Car | Winter | No | Art | Other | Fly |
| 9 | Car | Summer | No | Physical education | Pop | Fly |
| 10 | Car | Spring | No | Mathematics and statistics | Pop | Telepathy |
| 11 | Car | Summer | Yes | History | Rap/Hip hop | Invisibility |
| 12 | Car | Spring | No | Art | Rap/Hip hop | Freeze time |
| 13 | Bus | Winter | No | Computers and technology | Rap/Hip hop | Fly |
| 14 | Car | Winter | Yes | Social studies | Rap/Hip hop | Fly |
| 15 | Car | Summer | No | Art | Pop | Freeze time |
| 16 | Car | Fall | No | Mathematics and statistics | Pop | Fly |
| 17 | Bus | Winter | No | Science | Rap/Hip hop | Freeze time |
| 18 | Car | Spring | Yes | Art | Pop | Telepathy |
| 19 | Car | Fall | Yes | Science | Pop | Telepathy |
| 20 | Car | Summer | Yes | Physical education | Rap/Hip hop | Invisibility |
| 21 | Car | Spring | Yes | Science | Pop | Invisibility |
| 22 | Car | Winter | Yes | Mathematics and statistics | Country | Invisibility |
| 23 | Car | Summer | Yes | Art | Pop | Invisibility |
| 24 | Bus | Winter | Yes | Other | Pop | Telepathy |
| 25 | Bus | Summer | Yes | Science | Other | Fly |
| 26 | Car | Summer | No | Science | Pop | Fly |
| 27 | Car | Summer | Yes | Music | Pop | Telepathy |
| 28 | Car | Summer | No | Physical education | Country | Super strength |
| 29 | Car | Fall | Yes | Mathematics and statistics | Country | Telepathy |
| 30 | Car | Summer | Yes | Physical education | Rap/Hip hop | Telepathy |
| 31 | Boat | Winter | No | Computers and technology | Gospel | Invisibility |
| 32 | Car | Spring | No | Physical education | Pop | Fly |
| 33 | Car | Spring | No | Physical education | Pop | Fly |
| 34 | Car | Summer | No | Mathematics and statistics | Classical | Fly |
| 35 | Car | Fall | Yes | Science | Jazz | Telepathy |
| 36 | Car | Spring | No | Science | Rap/Hip hop | Telepathy |
| 37 | Car | Summer | No | Music | Country | Telepathy |
| 38 | Bus | Winter | No | Mathematics and statistics | Pop | Fly |
| 39 | Car | Spring | No | Art | Classical | Freeze time |
| 40 | Car | Winter | Yes | Art | Pop | Fly |
| 41 | Walk | Summer | Yes | Physical education | Rap/Hip hop | Fly |
| 42 | Bus | Winter | Yes | Physical education | Gospel | Invisibility |


| 43 | Bus | Summer | No | Art | Other | Invisibility |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 44 | Car | Summer | Yes | Computers and technology | Other | Freeze time |
| 45 | Car | Fall | Yes | Science | Pop | Fly |
| 46 | Car | Summer | Yes | Music | Rap/Hip hop | Fly |
| 47 | Car | Spring | No | Science | Rap/Hip hop | Invisibility |
| 48 | Bus | Spring | No | Music | Pop | Telepathy |
| 49 | Car | Summer | Yes | Social studies | Techno/ Electronic | Telepathy |
| 50 | Car | Summer | Yes | Physical education | Pop | Telepathy |
| 51 | Car | Spring | Yes | Other | Other | Telepathy |
| 52 | Car | Summer | No | Art | Pop | Fly |
| 53 | Car | Summer | Yes | Other | Pop | Telepathy |
| 54 | Car | Summer | Yes | Physical education | Rap/Hip hop | Invisibility |
| 55 | Bus | Summer | Yes | Physical education | Other | Super strength |
| 56 | Car | Summer | No | Science | Rap/Hip hop | Invisibility |
| 57 | Car | Winter | No | Languages | Rap/Hip hop | Super strength |
| 58 | Car | Fall | Yes | English | Pop | Fly |
| 59 | Car | Winter | No | Science | Pop | Telepathy |
| 60 | Car | Summer | No | Art | Pop | Invisibility |
| 61 | Car | Summer | Yes | Other | Pop | Freeze time |
| 62 | Bus | Spring | No | Science | Pop | Fly |
| 63 | Car | Winter | Yes | Mathematics and statistics | Other | Freeze time |
| 64 | Car | Summer | No | Social studies | Classical | Fly |
| 65 | Car | Winter | Yes | Science | Pop | Telepathy |
| 66 | Car | Winter | No | Science | Rock and roll | Fly |
| 67 | Car | Summer | No | Mathematics and statistics | Rap/Hip hop | Super strength |
| 68 | Car | Fall | No | Music | Rock and roll | Super strength |
| 69 | Car | Spring | No | Other | Other | Invisibility |
| 70 | Car | Summer | Yes | Mathematics and statistics | Rap/Hip hop | Telepathy |
| 71 | Car | Winter | No | Art | Other | Fly |
| 72 | Car | Spring | Yes | Mathematics and statistics | Pop | Telepathy |
| 73 | Car | Winter | Yes | Computers and technology | Techno/ Electronic | Telepathy |
| 74 | Walk | Winter | No | Physical education | Techno/ Electronic | Fly |
| 75 | Walk | Summer | No | History | Rock and roll | Fly |
| 76 | Skateboard/ Scooter/ Rollerblade | Winter | Yes | Computers and technology | Techno/ <br> Electronic | Freeze time |
| 77 | Car | Spring | Yes | Science | Other | Telepathy |
| 78 | Car | Summer | No | Music | Rap/Hip hop | Invisibility |
| 79 | Car | Summer | No | Social studies | Pop | Invisibility |
| 80 | Car | Summer | No | Other | Rap/Hip hop | Telepathy |
| 81 | Walk | Spring | Yes | History | Rap/Hip hop | Invisibility |
| 82 | Car | Summer | No | Art | Pop | Invisibility |


| 83 | Walk | Spring | No | Languages | Jazz | Super strength |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 84 | Car | Fall | No | History | Jazz | Invisibility |
| 85 | Car | Summer | No | Physical education | Rap/Hip hop | Freeze time |
| 86 | Car | Spring | No | Mathematics and statistics | Pop | Freeze time |
| 87 | Bus | Spring | Yes | Art | Pop | Telepathy |
| 88 | Car | Winter | No | Mathematics and statistics | Other | Invisibility |
| 89 | Car | Summer | Yes | Physical education | Country | Telepathy |
| 90 | Bus | Summer | No | Computers and technology | Other | Fly |
| 91 | Car | Winter | No | History | Pop | Telepathy |
| 92 | Walk | Winter | No | Science | Classical | Telepathy |
| 93 | Bicycle | Summer | No | Physical education | Pop | Invisibility |
| 94 | Car | Summer | No | English | Pop | Telepathy |
| 95 | Car | Summer | Yes | Physical education | Pop | Fly |
| 96 | Car | Winter | No | Science | Other | Freeze time |
| 97 | Car | Winter | No | Other | Rap/Hip hop | Super strength |
| 98 | Car | Summer | Yes | Physical education | Rap/Hip hop | Freeze time |
| 99 | Car | Spring | No | Music | Classical | Telepathy |
| 100 | Car | Spring | Yes | Science | Gospel | Telepathy |
| 101 | Car | Summer | Yes | History | Pop | Super strength |
| 102 | Car | Winter | Yes | English | Country | Freeze time |
| 103 | Car | Spring | No | Computers and technology | Other | Telepathy |
| 104 | Car | Winter | No | History | Other | Invisibility |
| 105 | Car | Fall | No | Music | Pop | Telepathy |
| 106 | Car | Fall | No | Science | Pop | Telepathy |
| 107 | Car | Winter | No | Art | Heavy metal | Fly |
| 108 | Car | Spring | Yes | Science | Rock and roll | Fly |
| 109 | Car | Fall | Yes | Music | Other | Fly |
| 110 | Car | Summer | Yes | Social studies | Techno/ <br> Electronic | Telepathy |
| 111 | Car | Spring | No | Physical education | Pop | Fly |
| 112 | Car | Summer | No | Physical education | Pop | Fly |
| 113 | Car | Summer | Yes | Social studies | Pop | Freeze time |
| 114 | Car | Summer | Yes | Computers and technology | Gospel | Freeze time |
| 115 | Car | Winter | Yes | Other | Rap/Hip hop | Telepathy |
| 116 | Car | Summer | Yes | Science | Country | Telepathy |
| 117 | Car | Fall |  | Music | Country | Fly |
| 118 | Walk | Summer | No | History | Pop | Telepathy |
| 119 | Car | Spring | Yes | Art | Pop | Freeze time |
| 120 | Car | Fall | Yes | Physical education | Rap/Hip hop | Fly |
| 121 | Car | Spring | No | Music | Rock and roll | Telepathy |
| 122 | Car | Fall | No | Art | Pop | Invisibility |
| 123 | Car | Summer | Yes | Physical education | Rap/Hip hop | Fly |
| 124 | Walk | Summer | No | Computers and technology | Pop | Telepathy |
| 125 | Car | Fall | No | Art | Pop | Fly |


| 126 | Bicycle | Spring | No | Science | Pop | Invisibility |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 127 | Car | Summer | No | Social studies | Gospel | Fly |
| 128 | Bicycle | Winter | No | Social studies | Rap/Hip hop | Fly |
| 129 | Car | Summer | Yes | Mathematics and statistics | Pop | Invisibility |
| 130 | Car | Fall | Yes | Mathematics and statistics | Country | Telepathy |
| 131 | Car | Winter | Yes | Music | Gospel | Super strength |
| 132 | Rail <br> (Train/Tram/ Subway) | Fall | Yes | Art | Other | Fly |
| 133 | Walk | Summer | No | Social studies | Pop | Invisibility |
| 134 | Car | Summer | Yes | Music | Pop | Freeze time |
| 135 | Car | Winter | No | Mathematics and statistics | Pop | Telepathy |
| 136 | Car | Fall | Yes | Music | Pop | Telepathy |
| 137 | Car | Summer | Yes | Computers and technology | Other | Freeze time |
| 138 | Car | Summer | Yes | Physical education | Pop | Telepathy |
| 139 | Car | Summer | Yes | Social studies | Other | Telepathy |
| 140 | Car | Spring | Yes | Physical education | Other | Freeze time |
| 141 | Car | Fall | Yes | Science | Country | Telepathy |
| 142 | Car | Spring | Yes | Science | Pop | Invisibility |
| 143 | Car | Summer | No | Other | Rap/Hip hop | Freeze time |
| 144 | Car | Summer | No | Other | Other | Fly |
| 145 | Car | Summer | No | Languages | Pop | Freeze time |
| 146 | Car | Summer | Yes | Physical education | Pop | Telepathy |
| 147 | Bus | Winter | No | History | Country | Invisibility |
| 148 | Car | Spring | No | Computers and technology | Other | Telepathy |
| 149 | Bus | Winter | Yes | Science | Pop | Invisibility |
| 150 | Car | Summer | No | Social studies | Rap/Hip hop | Invisibility |
| 151 | Car | Summer | No | Physical education | Pop | Invisibility |
| 152 | Car | Summer | Yes | Physical education | Pop | Super strength |
| 153 | Car | Summer | No | Mathematics and statistics | Pop | Fly |
| 154 | Car | Summer | No | Art | Rap/Hip hop | Freeze time |
| 155 | Car | Winter | Yes | Other | Classical | Freeze time |
| 156 | Car | Summer | Yes | Computers and technology | Other | Telepathy |
| 157 | Car | Spring | No | Other | Pop | Freeze time |
| 158 | Car | Winter | Yes | Music | Country | Fly |
| 159 | Car | Winter | No | History | Jazz | Invisibility |
| 160 | Car | Spring | Yes | History | Pop | Fly |
| 161 | Car | Winter | Yes | Mathematics and statistics | Other | Telepathy |
| 162 | Car | Fall | No | Science | Country | Invisibility |
| 163 | Car | Winter | No | Science | Other | Fly |
| 164 | Car | Summer | No | Science | Pop | Fly |
| 165 | Skateboard/ Scooter/ Rollerblade | Spring | Yes | Social studies | Other | Freeze time |
| 166 | Car | Winter | Yes | Art | Rap/Hip hop | Fly |


| 167 | Car | Summer | Yes | Other | Pop | Freeze time |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 168 | Car | Summer | No | English | Pop | Telepathy |
| 169 | Car | Summer | No | Other | Pop | Invisibility |
| 170 | Car | Summer | Yes | Physical education | Techno/ Electronic | Freeze time |
| 171 | Car | Summer | No | Art | Pop | Telepathy |
| 172 | Car | Summer | No | Physical education | Rap/Hip hop | Freeze time |
| 173 | Car | Winter | Yes | Mathematics and statistics | Other | Invisibility |
| 174 | Bus | Summer | Yes | Music | Pop | Freeze time |
| 175 | Car | Winter | No | Art | Pop | Fly |
| 176 | Car | Fall | No | Science | Rap/Hip hop | Fly |
| 177 | Car | Winter | Yes | Social studies | Pop | Telepathy |
| 178 | Car | Fall | No | Art | Other | Fly |
| 179 | Bus | Spring | No | Physical education | Country | Fly |
| 180 | Car | Winter | No | Music | Other | Telepathy |
| 181 | Bus | Summer | No | Computers and technology | Rap/Hip hop | Freeze time |
| 182 | Car | Summer | Yes | Physical education | Rap/Hip hop | Invisibility |
| 183 | Car | Summer | Yes | Music | Other | Telepathy |
| 184 | Car | Spring | No | Science | Rap/Hip hop | Invisibility |
| 185 | Rail (Train/Tram/ Subway) | Summer | No | Physical education | Other | Freeze time |
| 186 | Car | Summer | Yes | Mathematics and statistics | Rap/Hip hop | Fly |
| 187 | Bus | Winter | Yes | Mathematics and statistics | Other | Super strength |
| 188 | Car | Summer | No | Mathematics and statistics | Other | Freeze time |
| 189 | Rail (Train/Tram/ Subway) | Fall | Yes | Music | Jazz | Fly |
| 190 | Car | Summer | Yes | Science | Pop | Super strength |
| 191 | Car | Summer | Yes | Science | Techno/ Electronic | Freeze time |
| 192 | Car | Spring | Yes | Physical education | Rap/Hip hop | Freeze time |
| 193 | Car | Summer | Yes | Physical education | Rap/Hip hop | Freeze time |
| 194 | Car | Winter | No | Physical education | Rap/Hip hop | Telepathy |
| 195 | Car | Winter | No | Music | Jazz | Freeze time |
| 196 | Walk | Summer | Yes | History | Country | Freeze time |
| 197 | Car | Spring | No | History | Rap/Hip hop | Freeze time |
| 198 | Car | Fall | Yes | Other | Pop | Freeze time |
| 199 | Car | Spring | Yes | Science | Other | Freeze time |
| 200 | Bicycle | Winter | Yes | Other | Rap/Hip hop | Freeze time |

Name $\qquad$ Date $\qquad$

## Lesson 21: Why Worry About Sampling Variability?

Exit Ticket

How is a meaningful difference in sample means different from a non-meaningful difference in sample means? You may use what you saw in the dot plots of this lesson to help you answer this question.

Template for Bags $A$ and $B$

| 5 | 5 | 5 | 5 | 5 | 6 | 6 | 6 | 6 | 6 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 7 | 7 | 7 | 7 | 7 | 8 | 8 | 8 | 8 | 8 |
| 9 | 9 | 9 | 9 | 9 | 10 | 10 | 10 | 10 | 10 |
| 11 | 11 | 11 | 11 | 11 | 12 | 12 | 12 | 12 | 12 |
| 13 | 13 | 13 | 13 | 13 | 14 | 14 | 14 | 14 | 14 |
| 15 | 15 | 15 | 15 | 15 | 16 | 16 | 16 | 16 | 16 |
| 17 | 17 | 17 | 17 | 17 | 18 | 18 | 18 | 18 | 18 |
| 19 | 19 | 19 | 19 | 19 | 20 | 20 | 20 | 20 | 20 |
| 21 | 21 | 21 | 21 | 21 | 22 | 22 | 22 | 22 | 22 |
| 23 | 23 | 23 | 23 | 23 | 24 | 24 | 24 | 24 | 24 |

## Template for Bag C

| 1 | 1 | 1 | 1 | 1 | 2 | 2 | 2 | 2 | 2 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 3 | 3 | 3 | 3 | 3 | 4 | 4 | 4 | 4 | 4 |
| 5 | 5 | 5 | 5 | 5 | 6 | 6 | 6 | 6 | 6 |
| 7 | 7 | 7 | 7 | 7 | 8 | 8 | 8 | 8 | 8 |
| 9 | 9 | 9 | 9 | 9 | 10 | 10 | 10 | 10 | 10 |
| 11 | 11 | 11 | 11 | 11 | 12 | 12 | 12 | 12 | 12 |
| 13 | 13 | 13 | 13 | 13 | 14 | 14 | 14 | 14 | 14 |
| 15 | 15 | 15 | 15 | 15 | 16 | 16 | 16 | 16 | 16 |
| 17 | 17 | 17 | 17 | 17 | 18 | 18 | 18 | 18 | 18 |
| 19 | 19 | 19 | 19 | 19 | 20 | 20 | 20 | 20 | 20 |

$\qquad$ Date $\qquad$

## Lesson 22: Using Sample Data to Compare the Means of Two or

## More Populations

## Exit Ticket

Suppose that Brett randomly sampled 12 tenth-grade girls and boys in his school district and asked them for the number of minutes per day that they text. The data and summary measures follow.

| Gender | Number of Minutes of Texting |  |  |  |  |  |  |  |  |  | Mean | MAD |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Girls | 98 | 104 | 95 | 101 | 98 | 107 | 86 | 92 | 96 | 107 | 88 | 95 |  | 97.3 |
| Boys | 66 | 72 | 65 | 60 | 78 | 82 | 63 | 56 | 85 | 79 | 68 | 77 |  | 70.9 |

1. Draw dot plots for the two data sets using the same numerical scales. Discuss the amount of overlap between the two dot plots that you drew and what it may mean in the context of the problem.
2. Compare the variability in the two data sets using the MAD. Interpret the result in the context of the problem.
3. From 1 and 2, does the difference in the two means appear to be meaningful? Explain.
$\qquad$

## Lesson 23: Using Sample Data to Compare the Means of Two or

## More Populations

## Exit Ticket

1. Do eleventh-grade males text more per day than eleventh-grade females do? To answer this question, two randomly selected samples were obtained from the Excel data file used in this lesson. Indicate how 20 randomly selected eleventh-grade females would be chosen for this study. Indicate how 20 randomly selected eleventh-grade males would be chosen.
2. Two randomly selected samples (one of eleventh-grade females and one of eleventh-grade males) were obtained from the database. The results are indicated below:

|  | Mean number of minutes <br> per day texting | MAD (minutes) |
| :---: | :---: | :---: |
| Eleventh-grade females | 102.55 | 1.31 |
| Eleventh-grade males | 100.32 | 1.12 |

Is there a meaningful difference in the number of minutes per day that eleventh-grade females and males text? Explain your answer.

Copy of the Excel student data file

| ID Number | Texting | ReacTime | Homework | Sleep |
| :---: | :---: | :---: | :---: | :---: |
| 1 | 99 | 0.33 | 9.0 | 8.2 |
| 2 | 69 | 0.39 | 8.6 | 7.5 |
| 3 | 138 | 0.36 | 6.1 | 8.7 |
| 4 | 100 | 0.40 | 7.9 | 7.8 |
| 5 | 116 | 0.28 | 5.1 | 8.8 |
| 6 | 112 | 0.38 | 6.5 | 7.9 |
| 7 | 79 | 0.35 | 6.5 | 8.8 |
| 8 | 111 | 0.41 | 8.8 | 8.5 |
| 9 | 115 | 0.49 | 8.4 | 8.4 |
| 10 | 82 | 0.43 | 8.7 | 8.8 |
| 11 | 136 | 0.46 | 7.2 | 8.4 |
| 12 | 112 | 0.51 | 8.3 | 9.0 |
| 13 | 101 | 0.42 | 7.0 | 8.8 |
| 14 | 89 | 0.38 | 5.6 | 8.3 |
| 15 | 120 | 0.35 | 7.2 | 8.2 |
| 16 | 144 | 0.36 | 3.9 | 8.8 |
| 17 | 131 | 0.26 | 9.0 | 8.9 |
| 18 | 126 | 0.39 | 7.0 | 8.5 |
| 19 | 118 | 0.37 | 9.2 | 8.7 |
| 20 | 83 | 0.34 | 7.4 | 8.6 |
| 21 | 120 | 0.20 | 4.5 | 8.7 |
| 22 | 114 | 0.38 | 6.0 | 8.6 |
| 23 | 90 | 0.25 | 7.0 | 8.4 |
| 24 | 116 | 0.36 | 5.8 | 8.4 |
| 25 | 108 | 0.36 | 8.9 | 8.1 |
| 26 | 89 | 0.31 | 8.4 | 8.8 |
| 27 | 124 | 0.44 | 6.3 | 8.3 |
| 28 | 121 | 0.32 | 5.2 | 8.0 |
| 29 | 104 | 0.30 | 6.7 | 8.1 |
| 30 | 110 | 0.39 | 7.8 | 8.1 |
| 31 | 119 | 0.36 | 8.5 | 8.0 |
| 32 | 113 | 0.40 | 5.3 | 9.4 |
| 33 | 106 | 0.36 | 5.7 | 8.6 |
| 34 | 119 | 0.33 | 5.9 | 8.4 |
| 35 | 129 | 0.38 | 6.2 | 9.0 |
| 36 | 95 | 0.44 | 7.9 | 8.3 |
| 37 | 126 | 0.41 | 7.2 | 8.6 |


| 38 | 106 | 0.26 | 7.1 | 8.5 |
| :---: | :---: | :---: | :---: | :---: |
| 39 | 116 | 0.34 | 4.9 | 8.4 |
| 40 | 107 | 0.35 | 9.3 | 8.1 |
| 41 | 108 | 0.48 | 8.1 | 8.6 |
| 42 | 97 | 0.40 | 7.1 | 8.8 |
| 43 | 97 | 0.27 | 4.2 | 8.3 |
| 44 | 100 | 0.24 | 6.2 | 8.9 |
| 45 | 123 | 0.50 | 8.1 | 8.6 |
| 46 | 94 | 0.39 | 5.2 | 8.3 |
| 47 | 87 | 0.37 | 8.0 | 8.3 |
| 48 | 93 | 0.42 | 9.7 | 8.1 |
| 49 | 117 | 0.39 | 7.9 | 8.3 |
| 50 | 94 | 0.36 | 6.9 | 8.9 |
| 51 | 124 | 0.29 | 8.1 | 8.4 |
| 52 | 116 | 0.44 | 4.9 | 8.2 |
| 53 | 137 | 0.25 | 9.1 | 8.3 |
| 54 | 123 | 0.30 | 3.8 | 8.7 |
| 55 | 122 | 0.21 | 6.6 | 8.8 |
| 56 | 92 | 0.41 | 7.6 | 8.6 |
| 57 | 101 | 0.36 | 8.5 | 8.2 |
| 58 | 111 | 0.34 | 6.5 | 8.7 |
| 59 | 126 | 0.31 | 5.6 | 8.6 |
| 60 | 81 | 0.33 | 7.3 | 8.4 |
| 61 | 118 | 0.35 | 8.4 | 8.3 |
| 62 | 113 | 0.37 | 7.7 | 8.4 |
| 63 | 114 | 0.49 | 6.9 | 8.6 |
| 64 | 124 | 0.34 | 8.5 | 8.1 |
| 65 | 90 | 0.48 | 6.6 | 8.7 |
| 66 | 99 | 0.39 | 6.5 | 8.5 |
| 67 | 155 | 0.40 | 6.5 | 9.0 |
| 68 | 77 | 0.45 | 4.9 | 8.3 |
| 69 | 79 | 0.23 | 7.7 | 8.6 |
| 70 | 91 | 0.43 | 6.7 | 8.9 |
| 71 | 107 | 0.42 | 6.9 | 8.6 |
| 72 | 112 | 0.39 | 6.3 | 8.6 |
| 73 | 147 | 0.34 | 7.8 | 8.3 |
| 74 | 126 | 0.52 | 9.2 | 8.9 |
| 75 | 106 | 0.27 | 6.7 | 8.0 |
| 76 | 86 | 0.21 | 6.1 | 8.4 |
| 77 | 111 | 0.29 | 7.4 | 8.0 |
| 78 | 118 | 0.41 | 5.2 | 8.8 |


| 79 | 105 | 0.28 | 5.9 | 8.3 |
| :---: | :---: | :---: | :---: | :---: |
| 80 | 108 | 0.40 | 7.0 | 8.6 |
| 81 | 131 | 0.32 | 7.5 | 8.5 |
| 82 | 86 | 0.34 | 7.4 | 8.4 |
| 83 | 87 | 0.27 | 7.7 | 8.6 |
| 84 | 116 | 0.34 | 9.6 | 9.1 |
| 85 | 102 | 0.42 | 5.6 | 8.7 |
| 86 | 105 | 0.41 | 8.2 | 8.2 |
| 87 | 96 | 0.33 | 4.9 | 8.4 |
| 88 | 90 | 0.20 | 7.5 | 8.6 |
| 89 | 109 | 0.39 | 6.0 | 8.5 |
| 90 | 103 | 0.36 | 5.7 | 9.1 |
| 91 | 98 | 0.26 | 5.5 | 8.4 |
| 92 | 103 | 0.41 | 8.2 | 8.0 |
| 93 | 110 | 0.39 | 9.2 | 8.4 |
| 94 | 101 | 0.39 | 8.8 | 8.6 |
| 95 | 101 | 0.40 | 6.1 | 9.0 |
| 96 | 98 | 0.22 | 7.0 | 8.6 |
| 97 | 105 | 0.43 | 8.0 | 8.5 |
| 98 | 110 | 0.33 | 8.0 | 8.8 |
| 99 | 104 | 0.45 | 9.6 | 8.5 |
| 100 | 119 | 0.29 | 7.2 | 9.1 |
| 101 | 120 | 0.48 | 6.7 | 8.4 |
| 102 | 109 | 0.36 | 6.8 | 8.5 |
| 103 | 105 | 0.29 | 8.6 | 8.6 |
| 104 | 110 | 0.29 | 7.1 | 8.9 |
| 105 | 116 | 0.41 | 6.7 | 8.8 |
| 106 | 114 | 0.25 | 9.0 | 8.8 |
| 107 | 111 | 0.35 | 9.9 | 8.6 |
| 108 | 137 | 0.37 | 6.1 | 7.9 |
| 109 | 104 | 0.37 | 7.3 | 9.0 |
| 110 | 95 | 0.33 | 8.3 | 8.0 |
| 111 | 117 | 0.29 | 7.5 | 8.8 |
| 112 | 100 | 0.30 | 2.9 | 9.3 |
| 113 | 105 | 0.24 | 6.1 | 8.5 |
| 114 | 102 | 0.41 | 7.7 | 8.0 |
| 115 | 109 | 0.32 | 5.8 | 8.2 |
| 116 | 108 | 0.36 | 6.6 | 8.3 |
| 117 | 111 | 0.43 | 8.2 | 8.5 |
| 118 | 115 | 0.20 | 5.7 | 8.9 |
| 119 | 89 | 0.34 | 5.1 | 8.1 |


| 120 | 94 | 0.29 | 9.2 | 8.5 |
| :---: | :---: | :---: | :---: | :---: |
| 121 | 105 | 0.26 | 7.3 | 8.6 |
| 122 | 143 | 0.42 | 5.8 | 8.1 |
| 123 | 129 | 0.29 | 6.8 | 8.8 |
| 124 | 118 | 0.31 | 6.2 | 8.7 |
| 125 | 129 | 0.38 | 9.1 | 8.4 |
| 126 | 96 | 0.25 | 6.7 | 8.5 |
| 127 | 95 | 0.27 | 7.7 | 8.3 |
| 128 | 43 | 0.22 | 6.3 | 9.2 |
| 129 | 64 | 0.23 | 3.7 | 8.5 |
| 130 | 38 | 0.41 | 5.2 | 9.1 |
| 131 | 46 | 0.35 | 7.1 | 8.3 |
| 132 | 56 | 0.32 | 4.7 | 8.9 |
| 133 | 41 | 0.45 | 7.2 | 8.8 |
| 134 | 55 | 0.27 | 4.1 | 8.5 |
| 135 | 57 | 0.40 | 7.5 | 8.6 |
| 136 | 66 | 0.41 | 6.9 | 8.0 |
| 137 | 62 | 0.39 | 3.8 | 8.5 |
| 138 | 49 | 0.36 | 6.4 | 8.5 |
| 139 | 33 | 0.21 | 4.8 | 9.0 |
| 140 | 38 | 0.34 | 5.6 | 8.5 |
| 141 | 75 | 0.19 | 5.0 | 8.2 |
| 142 | 68 | 0.25 | 5.4 | 8.4 |
| 143 | 60 | 0.47 | 7.4 | 9.1 |
| 144 | 63 | 0.33 | 4.4 | 8.2 |
| 145 | 48 | 0.28 | 7.1 | 8.2 |
| 146 | 49 | 0.36 | 2.7 | 8.5 |
| 147 | 72 | 0.44 | 5.6 | 7.6 |
| 148 | 54 | 0.51 | 4.3 | 8.7 |
| 149 | 65 | 0.38 | 7.7 | 8.5 |
| 150 | 72 | 0.40 | 3.4 | 9.1 |
| 151 | 51 | 0.16 | 4.9 | 8.4 |
| 152 | 64 | 0.16 | 4.4 | 8.5 |
| 153 | 43 | 0.34 | 0.1 | 8.8 |
| 154 | 57 | 0.38 | 4.4 | 8.2 |
| 155 | 72 | 0.51 | 3.2 | 8.4 |
| 156 | 37 | 0.46 | 5.3 | 8.6 |
| 157 | 50 | 0.33 | 4.1 | 8.2 |
| 158 | 41 | 0.46 | 4.5 | 8.9 |
| 159 | 63 | 0.40 | 5.0 | 8.7 |
| 160 | 51 | 0.33 | 5.4 | 7.9 |


| 161 | 57 | 0.51 | 4.9 | 8.6 |
| :---: | :---: | :---: | :---: | :---: |
| 162 | 51 | 0.24 | 1.7 | 8.4 |
| 163 | 73 | 0.32 | 5.6 | 8.6 |
| 164 | 51 | 0.37 | 4.0 | 8.5 |
| 165 | 52 | 0.36 | 5.8 | 8.3 |
| 166 | 52 | 0.34 | 4.6 | 8.1 |
| 167 | 63 | 0.34 | 4.1 | 8.1 |
| 168 | 76 | 0.30 | 6.1 | 8.2 |
| 169 | 56 | 0.40 | 5.7 | 8.5 |
| 170 | 47 | 0.33 | 5.0 | 8.2 |
| 171 | 44 | 0.41 | 5.0 | 8.3 |
| 172 | 60 | 0.33 | 7.7 | 8.4 |
| 173 | 36 | 0.39 | 6.5 | 8.8 |
| 174 | 52 | 0.30 | 5.4 | 8.2 |
| 175 | 53 | 0.27 | 5.6 | 8.2 |
| 176 | 60 | 0.35 | 6.0 | 8.6 |
| 177 | 48 | 0.43 | 3.6 | 8.6 |
| 178 | 63 | 0.49 | 0.2 | 8.2 |
| 179 | 76 | 0.42 | 5.9 | 8.9 |
| 180 | 58 | 0.34 | 7.3 | 8.3 |
| 181 | 51 | 0.43 | 6.4 | 8.7 |
| 182 | 38 | 0.33 | 4.9 | 8.5 |
| 183 | 46 | 0.17 | 4.7 | 8.3 |
| 184 | 53 | 0.34 | 6.4 | 8.7 |
| 185 | 60 | 0.38 | 6.1 | 8.7 |
| 186 | 71 | 0.23 | 6.9 | 8.2 |
| 187 | 54 | 0.41 | 2.9 | 8.3 |
| 188 | 61 | 0.44 | 5.8 | 8.4 |
| 189 | 62 | 0.35 | 3.9 | 8.9 |
| 190 | 55 | 0.15 | 4.8 | 8.0 |
| 191 | 57 | 0.22 | 4.1 | 8.2 |
| 192 | 43 | 0.41 | 7.5 | 8.5 |
| 193 | 51 | 0.34 | 2.4 | 8.6 |
| 194 | 34 | 0.55 | 3.5 | 8.4 |
| 195 | 38 | 0.43 | 7.1 | 8.8 |
| 196 | 49 | 0.38 | 3.5 | 8.3 |
| 197 | 57 | 0.30 | 3.6 | 8.5 |
| 198 | 53 | 0.37 | 5.2 | 9.1 |
| 199 | 51 | 0.36 | 5.1 | 8.2 |
| 200 | 59 | 0.38 | 3.6 | 8.7 |
| 201 | 35 | 0.44 | 4.0 | 8.0 |


| 202 | 73 | 0.32 | 3.0 | 8.3 |
| :---: | :---: | :---: | :---: | :---: |
| 203 | 68 | 0.37 | 2.7 | 8.4 |
| 204 | 31 | 0.36 | 4.6 | 8.6 |
| 205 | 40 | 0.33 | 9.0 | 8.3 |
| 206 | 60 | 0.36 | 6.6 | 8.5 |
| 207 | 66 | 0.44 | 4.2 | 8.5 |
| 208 | 47 | 0.22 | 4.5 | 8.7 |
| 209 | 56 | 0.30 | 4.8 | 8.6 |
| 210 | 72 | 0.36 | 2.9 | 8.8 |
| 211 | 68 | 0.50 | 6.6 | 8.3 |
| 212 | 45 | 0.37 | 7.3 | 8.5 |
| 213 | 58 | 0.17 | 4.9 | 9.0 |
| 214 | 64 | 0.34 | 3.2 | 8.6 |
| 215 | 66 | 0.34 | 2.5 | 8.4 |
| 216 | 49 | 0.29 | 5.0 | 8.3 |
| 217 | 83 | 0.39 | 2.5 | 8.8 |
| 218 | 73 | 0.33 | 3.6 | 8.4 |
| 219 | 52 | 0.34 | 3.3 | 8.8 |
| 220 | 56 | 0.28 | 8.8 | 8.7 |
| 221 | 58 | 0.32 | 5.6 | 8.3 |
| 222 | 53 | 0.40 | 5.9 | 8.1 |
| 223 | 50 | 0.23 | 4.4 | 8.4 |
| 224 | 43 | 0.34 | 3.9 | 8.7 |
| 225 | 50 | 0.39 | 4.4 | 8.0 |
| 226 | 44 | 0.31 | 4.4 | 8.4 |
| 227 | 59 | 0.36 | 6.0 | 9.1 |
| 228 | 41 | 0.35 | 3.2 | 8.4 |
| 229 | 53 | 0.29 | 6.6 | 8.7 |
| 230 | 49 | 0.37 | 5.7 | 8.3 |
| 231 | 42 | 0.22 | 8.5 | 8.6 |
| 232 | 48 | 0.34 | 3.9 | 8.2 |
| 233 | 60 | 0.31 | 6.1 | 8.8 |
| 234 | 56 | 0.50 | 2.6 | 8.5 |
| 235 | 43 | 0.25 | 5.3 | 8.9 |
| 236 | 67 | 0.32 | 6.1 | 8.8 |
| 237 | 43 | 0.24 | 8.6 | 8.8 |
| 238 | 41 | 0.46 | 5.1 | 8.7 |
| 239 | 66 | 0.45 | 4.9 | 8.3 |
| 240 | 44 | 0.52 | 4.1 | 8.7 |
| 241 | 70 | 0.43 | 6.6 | 8.8 |
| 242 | 63 | 0.38 | 7.9 | 8.4 |


| 243 | 47 | 0.24 | 3.9 | 8.3 |
| :---: | :---: | :---: | :---: | :---: |
| 244 | 52 | 0.38 | 5.4 | 8.8 |
| 245 | 49 | 0.47 | 4.2 | 8.4 |
| 246 | 45 | 0.31 | 8.1 | 8.8 |
| 247 | 46 | 0.37 | 1.9 | 8.3 |
| 248 | 19 | 0.31 | 6.5 | 8.3 |
| 249 | 63 | 0.40 | 6.1 | 8.5 |
| 250 | 64 | 0.35 | 5.8 | 8.1 |
| 251 | 63 | 0.34 | 6.7 | 8.5 |
| 252 | 68 | 0.46 | 6.9 | 8.5 |
| 253 | 48 | 0.43 | 8.6 | 8.7 |
| 254 | 43 | 0.38 | 4.4 | 8.3 |
| 255 | 50 | 0.32 | 4.6 | 8.7 |
| 256 | 76 | 0.31 | 4.0 | 8.3 |
| 257 | 64 | 0.39 | 5.7 | 8.6 |
| 258 | 38 | 0.29 | 6.4 | 8.0 |
| 259 | 90 | 0.30 | 7.0 | 8.6 |
| 260 | 37 | 0.39 | 4.8 | 8.8 |
| 261 | 58 | 0.37 | 6.5 | 8.0 |
| 262 | 42 | 0.27 | 4.5 | 8.6 |
| 263 | 58 | 0.37 | 6.0 | 8.3 |
| 264 | 42 | 0.42 | 7.2 | 8.8 |
| 265 | 66 | 0.33 | 12.6 | 8.8 |
| 266 | 116 | 0.44 | 8.7 | 7.5 |
| 267 | 76 | 0.43 | 9.5 | 6.9 |
| 268 | 125 | 0.46 | 9.9 | 6.8 |
| 269 | 128 | 0.41 | 9.8 | 6.6 |
| 270 | 128 | 0.37 | 11.3 | 7.1 |
| 271 | 125 | 0.44 | 6.7 | 7.9 |
| 272 | 80 | 0.49 | 10.6 | 7.1 |
| 273 | 110 | 0.48 | 9.9 | 7.2 |
| 274 | 135 | 0.41 | 9.8 | 7.8 |
| 275 | 136 | 0.45 | 8.9 | 7.2 |
| 276 | 142 | 0.43 | 10.2 | 8.0 |
| 277 | 120 | 0.48 | 10.2 | 7.5 |
| 278 | 109 | 0.43 | 10.1 | 7.1 |
| 279 | 109 | 0.50 | 10.9 | 7.5 |
| 280 | 111 | 0.35 | 11.8 | 7.4 |
| 281 | 101 | 0.49 | 8.5 | 7.8 |
| 282 | 98 | 0.50 | 11.6 | 7.2 |
| 283 | 91 | 0.56 | 10.0 | 7.3 |


| 284 | 151 | 0.50 | 7.7 | 6.7 |
| :---: | :---: | :---: | :---: | :---: |
| 285 | 82 | 0.48 | 14.0 | 7.5 |
| 286 | 107 | 0.48 | 9.5 | 7.5 |
| 287 | 83 | 0.40 | 12.0 | 7.2 |
| 288 | 91 | 0.40 | 9.2 | 7.9 |
| 289 | 127 | 0.40 | 9.1 | 7.6 |
| 290 | 115 | 0.42 | 11.6 | 6.8 |
| 291 | 118 | 0.40 | 9.8 | 7.3 |
| 292 | 89 | 0.42 | 10.8 | 7.0 |
| 293 | 100 | 0.46 | 11.6 | 7.3 |
| 294 | 97 | 0.39 | 8.5 | 7.8 |
| 295 | 110 | 0.36 | 11.1 | 7.7 |
| 296 | 88 | 0.40 | 9.0 | 6.7 |
| 297 | 103 | 0.47 | 11.7 | 6.7 |
| 298 | 82 | 0.49 | 10.7 | 7.5 |
| 299 | 87 | 0.41 | 8.1 | 7.4 |
| 300 | 130 | 0.39 | 9.8 | 7.6 |
| 301 | 116 | 0.42 | 9.6 | 7.6 |
| 302 | 96 | 0.42 | 11.8 | 7.1 |
| 303 | 122 | 0.39 | 7.9 | 7.1 |
| 304 | 70 | 0.38 | 11.1 | 7.4 |
| 305 | 116 | 0.47 | 8.8 | 7.3 |
| 306 | 122 | 0.48 | 9.0 | 7.0 |
| 307 | 109 | 0.45 | 10.0 | 7.3 |
| 308 | 114 | 0.50 | 10.1 | 7.3 |
| 309 | 62 | 0.47 | 11.4 | 7.3 |
| 310 | 120 | 0.51 | 9.5 | 6.3 |
| 311 | 130 | 0.38 | 10.5 | 7.7 |
| 312 | 92 | 0.47 | 11.8 | 7.3 |
| 313 | 81 | 0.55 | 7.9 | 7.3 |
| 314 | 82 | 0.51 | 10.1 | 7.7 |
| 315 | 102 | 0.48 | 10.9 | 6.5 |
| 316 | 113 | 0.43 | 10.2 | 7.9 |
| 317 | 119 | 0.43 | 8.0 | 6.8 |
| 318 | 108 | 0.48 | 8.9 | 7.0 |
| 319 | 130 | 0.53 | 8.3 | 7.3 |
| 320 | 111 | 0.50 | 9.9 | 6.6 |
| 321 | 132 | 0.50 | 11.5 | 6.8 |
| 322 | 110 | 0.47 | 10.8 | 7.1 |
| 323 | 95 | 0.49 | 10.4 | 7.5 |
| 324 | 137 | 0.29 | 9.8 | 7.5 |


| 325 | 98 | 0.53 | 11.5 | 7.0 |
| :---: | :---: | :---: | :---: | :---: |
| 326 | 124 | 0.55 | 10.2 | 6.6 |
| 327 | 146 | 0.36 | 10.2 | 7.5 |
| 328 | 126 | 0.51 | 10.6 | 6.5 |
| 329 | 124 | 0.53 | 9.4 | 7.6 |
| 330 | 99 | 0.47 | 8.7 | 7.7 |
| 331 | 100 | 0.51 | 9.5 | 7.9 |
| 332 | 101 | 0.45 | 9.5 | 7.1 |
| 333 | 113 | 0.37 | 9.4 | 7.8 |
| 334 | 139 | 0.42 | 8.9 | 7.1 |
| 335 | 105 | 0.38 | 8.7 | 7.4 |
| 336 | 113 | 0.45 | 10.7 | 7.3 |
| 337 | 104 | 0.45 | 9.6 | 7.2 |
| 338 | 117 | 0.48 | 10.3 | 7.3 |
| 339 | 132 | 0.43 | 10.9 | 7.7 |
| 340 | 100 | 0.44 | 11.8 | 6.8 |
| 341 | 109 | 0.40 | 8.1 | 7.2 |
| 342 | 95 | 0.39 | 9.7 | 7.4 |
| 343 | 139 | 0.39 | 9.8 | 7.7 |
| 344 | 140 | 0.47 | 8.9 | 7.3 |
| 345 | 110 | 0.48 | 12.1 | 7.2 |
| 346 | 97 | 0.56 | 11.5 | 8.2 |
| 347 | 98 | 0.49 | 11.2 | 6.9 |
| 348 | 146 | 0.44 | 10.0 | 7.2 |
| 349 | 92 | 0.47 | 12.0 | 6.5 |
| 350 | 128 | 0.43 | 10.8 | 7.7 |
| 351 | 156 | 0.50 | 11.4 | 6.3 |
| 352 | 134 | 0.39 | 9.1 | 8.2 |
| 353 | 110 | 0.44 | 7.6 | 6.6 |
| 354 | 104 | 0.45 | 12.4 | 7.5 |
| 355 | 98 | 0.54 | 11.0 | 7.1 |
| 356 | 120 | 0.50 | 10.5 | 7.3 |
| 357 | 140 | 0.50 | 10.6 | 6.9 |
| 358 | 130 | 0.53 | 10.7 | 7.4 |
| 359 | 115 | 0.45 | 10.1 | 7.1 |
| 360 | 159 | 0.41 | 10.7 | 7.5 |
| 361 | 114 | 0.43 | 9.9 | 6.9 |
| 362 | 128 | 0.46 | 9.3 | 7.0 |
| 363 | 96 | 0.49 | 7.6 | 7.5 |
| 364 | 61 | 0.49 | 12.0 | 6.7 |
| 365 | 60 | 0.46 | 8.2 | 7.6 |


| 366 | 51 | 0.50 | 7.8 | 7.6 |
| :---: | :---: | :---: | :---: | :---: |
| 367 | 61 | 0.49 | 7.9 | 7.1 |
| 368 | 46 | 0.57 | 7.5 | 6.5 |
| 369 | 60 | 0.44 | 8.0 | 7.7 |
| 370 | 53 | 0.36 | 12.5 | 7.1 |
| 371 | 55 | 0.45 | 10.7 | 7.3 |
| 372 | 59 | 0.38 | 9.0 | 7.0 |
| 373 | 61 | 0.38 | 9.3 | 6.9 |
| 374 | 69 | 0.57 | 10.4 | 7.4 |
| 375 | 63 | 0.51 | 10.6 | 7.0 |
| 376 | 62 | 0.48 | 12.8 | 7.1 |
| 377 | 57 | 0.49 | 7.8 | 7.4 |
| 378 | 70 | 0.40 | 11.2 | 6.9 |
| 379 | 31 | 0.46 | 9.2 | 6.6 |
| 380 | 70 | 0.41 | 10.8 | 6.8 |
| 381 | 66 | 0.39 | 10.9 | 7.8 |
| 382 | 62 | 0.51 | 9.8 | 6.3 |
| 383 | 75 | 0.50 | 9.6 | 7.2 |
| 384 | 58 | 0.34 | 9.1 | 7.2 |
| 385 | 50 | 0.47 | 11.3 | 7.3 |
| 386 | 73 | 0.44 | 9.1 | 7.4 |
| 387 | 61 | 0.37 | 10.8 | 7.2 |
| 388 | 48 | 0.48 | 8.1 | 6.8 |
| 389 | 54 | 0.52 | 12.4 | 7.6 |
| 390 | 63 | 0.52 | 9.4 | 7.1 |
| 391 | 69 | 0.35 | 13.2 | 7.1 |
| 392 | 71 | 0.39 | 12.0 | 7.6 |
| 393 | 44 | 0.40 | 10.6 | 7.4 |
| 394 | 60 | 0.42 | 11.8 | 6.8 |
| 395 | 79 | 0.37 | 9.4 | 7.9 |
| 396 | 38 | 0.50 | 9.9 | 7.3 |
| 397 | 80 | 0.57 | 11.0 | 7.0 |
| 398 | 54 | 0.46 | 8.8 | 6.9 |
| 399 | 74 | 0.44 | 10.8 | 7.6 |
| 400 | 37 | 0.40 | 9.3 | 7.8 |
| 401 | 69 | 0.47 | 9.8 | 7.1 |
| 402 | 54 | 0.47 | 9.6 | 7.3 |
| 403 | 68 | 0.42 | 10.1 | 8.1 |
| 404 | 49 | 0.56 | 8.9 | 7.2 |
| 405 | 55 | 0.45 | 6.1 | 7.2 |
| 406 | 64 | 0.43 | 10.2 | 6.9 |


| 407 | 83 | 0.41 | 7.3 | 6.6 |
| :---: | :---: | :---: | :---: | :---: |
| 408 | 36 | 0.46 | 11.5 | 7.3 |
| 409 | 44 | 0.43 | 11.0 | 6.7 |
| 410 | 65 | 0.44 | 11.1 | 7.0 |
| 411 | 77 | 0.39 | 12.1 | 7.7 |
| 412 | 33 | 0.44 | 6.9 | 7.1 |
| 413 | 45 | 0.47 | 8.2 | 6.9 |
| 414 | 70 | 0.53 | 7.3 | 7.2 |
| 415 | 77 | 0.44 | 8.9 | 7.2 |
| 416 | 53 | 0.46 | 9.2 | 6.8 |
| 417 | 60 | 0.49 | 11.0 | 7.4 |
| 418 | 86 | 0.44 | 5.8 | 7.8 |
| 419 | 49 | 0.55 | 8.4 | 7.2 |
| 420 | 50 | 0.45 | 12.3 | 6.5 |
| 421 | 64 | 0.41 | 10.7 | 7.2 |
| 422 | 57 | 0.45 | 7.0 | 7.1 |
| 423 | 56 | 0.40 | 12.1 | 6.5 |
| 424 | 41 | 0.45 | 12.7 | 7.2 |
| 425 | 50 | 0.50 | 8.3 | 6.8 |
| 426 | 63 | 0.45 | 11.6 | 7.4 |
| 427 | 44 | 0.43 | 7.7 | 7.1 |
| 428 | 51 | 0.42 | 10.3 | 7.5 |
| 429 | 51 | 0.50 | 8.7 | 7.1 |
| 430 | 54 | 0.43 | 8.4 | 7.2 |
| 431 | 45 | 0.44 | 7.0 | 6.9 |
| 432 | 65 | 0.46 | 10.5 | 7.5 |
| 433 | 60 | 0.45 | 7.4 | 7.1 |
| 434 | 52 | 0.42 | 4.1 | 7.1 |
| 435 | 50 | 0.49 | 11.2 | 6.9 |
| 436 | 61 | 0.52 | 10.7 | 6.7 |
| 437 | 42 | 0.43 | 9.2 | 6.8 |
| 438 | 42 | 0.50 | 11.4 | 6.8 |
| 439 | 66 | 0.47 | 7.9 | 7.2 |
| 440 | 65 | 0.43 | 9.2 | 7.1 |

Name $\qquad$ Date $\qquad$

Round all decimal answers to the nearest hundredth.

1. You and a friend decide to conduct a survey at your school to see whether students are in favor of a new dress code policy. Your friend stands at the school entrance and asks the opinions of the first 100 students who come to campus on Monday. You obtain a list of all students at the school and randomly select 60 to survey.
a. Your friend finds $34 \%$ of his sample in favor of the new dress code policy, but you find only $16 \%$. Which do you believe is more likely to be representative of the school population? Explain your choice.
b. Suppose $25 \%$ of the students at the school are in favor of the new dress code policy. Below is a dot plot of the proportion of students who favor the new dress code for each of 100 different random samples of 50 students at the school.


If you were to select a random sample of 50 students and ask them if they favor the new dress code, do you think that your sample proportion will be within 0.05 of the population proportion? Explain.
c. Suppose ten people each take a simple random sample of 100 students from the school and calculate the proportion in the sample who favors the new dress code. On the dot plot axis below, place 10 values that you think are most believable for the proportions you could obtain.

| 0.0 | 0.1 | 0.2 | 0.3 | 0.4 | 0.5 | 0.6 | 0.7 | 0.8 | 0.9 | 1.0 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $\leftarrow$ sample proportion in favor of dress code $\rightarrow$ |  |  |  |  |  |  |  |  |  |  |

Explain your reasoning.
2. Students in a random sample of 57 students were asked to measure their hand spans (distance from outside of thumb to outside of little finger when the hand is stretched out as far as possible). The graphs below show the results for the males and females.

a. Based on these data, do you think there is a difference between the population mean hand span for males and the population mean hand span for females? Justify your answer.
b. The same students were asked to measure their heights, with the results shown below.


Are these height data more or less convincing of a difference in the population mean height than the hand-span data are of a difference in population mean hand span? Explain.
3. A student purchases a bag of "mini" chocolate chip cookies, and after opening the bag, finds one cookie that does not contain any chocolate chips! The student then wonders how unlikely it is to randomly find a cookie with no chocolate chips for this brand.
a. Based on the bag of 30 cookies, estimate the probability of this company producing a cookie with no chocolate chips.
b. Suppose the cookie company claims that $90 \%$ of all cookies it produces contain chocolate chips. Explain how you could simulate randomly selecting 30 cookies (one bag) from such a population to determine how many of the sampled cookies do not contain chocolate chips. Explain the details of your method so it could be carried out by another person.
c. Now, explain how you could use simulation to estimate the probability of obtaining a bag of 30 cookies with exactly one cookie with no chocolate chips.
d. If $90 \%$ of the cookies made by this company contain chocolate chips, then the actual probability of obtaining a bag of 30 cookies with one chipless cookie equals 0.143 . Based on this result, would you advise this student to complain to the company about finding one cookie with no chocolate chips in her bag of 30 ? Explain.

