## Lesson 21: Mathematical Area Problems

## Classwork

Opening Exercise
Patty is interested in expanding her backyard garden. Currently, the garden plot has a length of ft . and a width of ft .
a. What is the current area of the garden?

Patty plans on extending the length of the plot by ft . and the width by ft .
b. What will the new dimensions of the garden be? What will the new area of the garden be?
c. Draw a diagram that shows the change in dimension and area of Patty's garden as she expands it. The diagram should show the original garden as well as the expanded garden.
d. Based on your diagram, can the area of the garden be found in a way other than by multiplying the length by the width?
e. Based on your diagram, how would the area of the original garden change if only the length increased by ft.? By how much would the area increase?
f. How would the area of the original garden change if only the width increased by ft.? By how much would the area increase?
g. Complete the following table with the numeric expression, area, and increase in area for each change in the dimensions of the garden.

| Dimensions of the garden | Numeric expression for the area <br> of the garden | Area of the garden | Increase in area of <br> the garden |
| :--- | :--- | :--- | :--- |
| Original garden with length of <br> ft and width of ft. |  |  |  |
| The original garden with length <br> extended by ft. and width <br> extended by ft. |  |  |  |
| The original garden with only <br> the length extended by ft. |  |  |  |
| The original garden with only <br> the width extended by ft. |  |  |  |

h. Will the increase in both the length and width by ft. and ft., respectively, mean that the original area will increase strictly by the areas found in parts (e) and (f)? If the area is increasing by more than the areas found in parts (e) and (f), explain what accounts for the additional increase.

## Example 1

Examine the change in dimension and area of the following square as it increases by units from a side length of units to a new side length of units. Observe the way the area is calculated for the new square. The lengths are given in units, and the areas of the rectangles and squares are given in units ${ }^{2}$.

a. Based on the example above, draw a diagram for a square with side length of units that is increasing by units. Show the area calculation for the larger square in the same way as in the example.
b. Draw a diagram for a square with side length of units that is increased by units. Show the area calculation for the larger square in the same way as in the example.
c. Generalize the pattern for the area calculation of a square that has an increase in dimension. Let the side length of the original square be units and the increase in length be by units to the length and width. Use the diagram below to guide your work.


## Example 2

Bobby draws a square that is units by units. He increases the length by units and the width by units.
a. Draw a diagram that models this scenario.
b. Assume the area of the large rectangle is
units ${ }^{2}$. Find the value of .

## Example 3

The dimensions of a square with side length units are increased. In this figure the indicated lengths are given in units, and the indicated areas are given in units ${ }^{2}$.

a. What are the dimensions of the large rectangle in the figure?
b. Use the expressions in your response from part (a) to write an equation for the area of the large rectangle, where represents area.
c. Use the areas of the sections within the diagram to express the area of the large rectangle.
d. What can be concluded from parts (b) and (c)?
e. Explain how the expressions
and
differ within the context of the area of the figure.

## Problem Set

1. A square with side length units is decreased by units in both length and width.


Use the diagram to express
in terms of the other , and by filling in the blanks below:
2. In Example 3(c) we generalized that

Use these results to evaluate the following expressions by writing , etc.:
a. Evaluate
b. Evaluate
c. Evaluate
3. Use the results of Problem Set 1 to evaluate
by writing
4. The figures below show that is equal to

a. Create a drawing to show that
b. Use the result in part (a),
i.
ii.
iii.
c. Use the fact that
to create a way to mentally square any two digit number ending in " ."
5. Create an area model for each product. Use the area model to write an equivalent expression that represents the area.
a.
b.
c. Based on the context of the area model, how do the expressions provided in parts (a) and (b) differ from the equivalent expression answers you found for each?
6. Use the distributive property to multiply the following expressions:
a.
b. ; draw a figure that models this multiplication problem.
c.
d.
e.
f.

