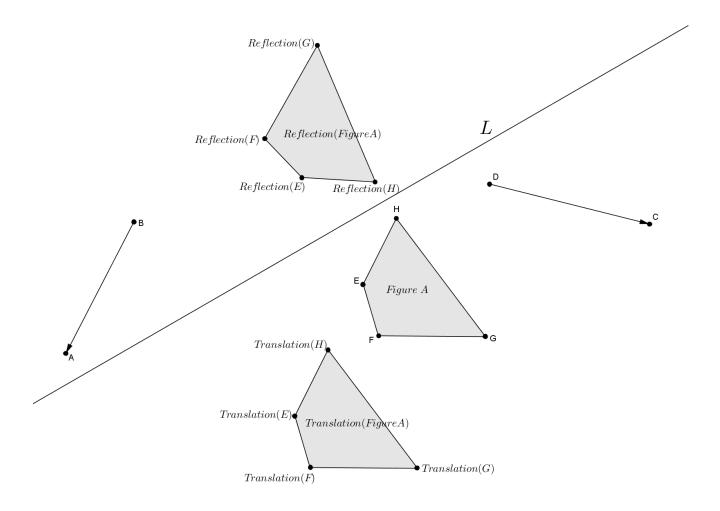
# **Lesson 8: Sequencing Reflections and Translations**

### Classwork

### Exercises 1–3

Use the figure below to answer Exercises 1–3.

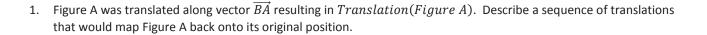




Sequencing Reflections and Translations 10/28/14







2. Figure A was reflected across line *L* resulting in *Reflection*(*Figure A*). Describe a sequence of reflections that would map Figure A back onto its original position.

3. Can *Translation*<sub> $\overline{BA}$ </sub> of Figure A undo the transformation of *Translation*<sub> $\overline{DC}$ </sub> of Figure A? Why or why not?



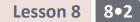


**S.40** 

Lesson 8

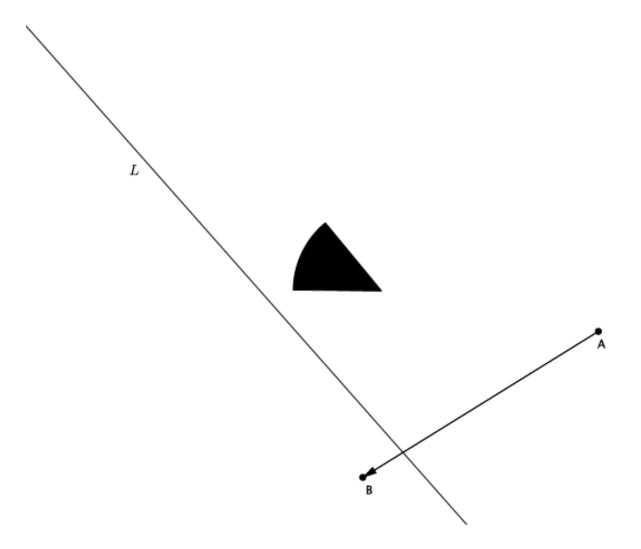
8•2





## Exercises 4–7

Let  ${\cal S}$  be the black figure.



- 4. Let there be the translation along vector AB and a reflection across line L.
  Use a transparency to perform the following sequence: Translate figure S; then, reflect figure S. Label the image S'.
- Let there be the translation along vector AB and a reflection across line L.
  Use a transparency to perform the following sequence: Reflect figure S; then, translate figure S. Label the image S''.



Sequencing Reflections and Translations 10/28/14

engage<sup>ny</sup>





6. Using your transparency, show that under a sequence of any two translations, *Translation* and *Translation*<sub>0</sub> (along different vectors), that the sequence of the *Translation* followed by the *Translation*<sub>0</sub> is equal to the sequence of the *Translation*<sub>0</sub> followed by the *Translation*. That is, draw a figure, *A*, and two vectors. Show that the translation along the first vector, followed by a translation along the second vector, places the figure in the same location as when you perform the translations in the reverse order. (This fact will be proven in high school). Label the transformed image *A*'. Now, draw two new vectors and translate along them just as before. This time, label the transformed image *A*''. Compare your work with a partner. Was the statement "the sequence of the *Translation*" true in all cases? Do you think it will always be true?

7. Does the same relationship you noticed in Exercise 6 hold true when you replace one of the translations with a reflection. That is, is the following statement true: A translation followed by a reflection is equal to a reflection followed by a translation?



Sequencing Reflections and Translations 10/28/14



S.42

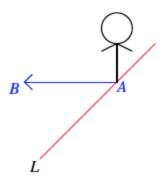
Lesson 8

**Lesson Summary** 

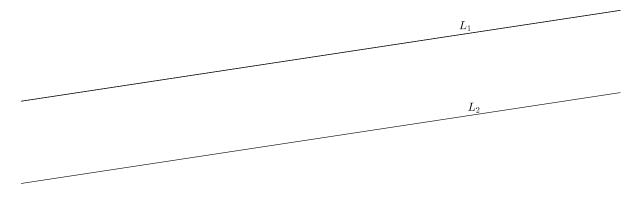
- A reflection across a line followed by a reflection across the same line places all figures in the plane back onto their original position.
- A reflection followed by a translation does not place a figure in the same location in the plane as a translation followed by a reflection. The order in which we perform a sequence of rigid motions matters.

#### **Problem Set**

1. Let there be a reflection across line L, and let there be a translation along vector  $\overrightarrow{AB}$ , as shown. If S denotes the black figure, compare the translation of S followed by the reflection of S with the reflection of S followed by the translation of S.



2. Let  $L_1$  and  $L_2$  be parallel lines, and let *Reflection*<sub>1</sub> and *Reflection*<sub>2</sub> be the reflections across  $L_1$  and  $L_2$ , respectively (in that order). Show that a  $Reflection_2$  followed by  $Reflection_1$  is not equal to a  $Reflection_1$  followed by  $Reflection_2$ . (Hint: Take a point on  $L_1$  and see what each of the sequences does to it.)



3. Let  $L_1$  and  $L_2$  be parallel lines, and let *Reflection*<sub>1</sub> and *Reflection*<sub>2</sub> be the reflections across  $L_1$  and  $L_2$ , respectively (in that order). Can you guess what Reflection<sub>1</sub> followed by Reflection<sub>2</sub> is? Give as persuasive an argument as you can. (Hint: Examine the work you just finished for the last problem.)



Sequencing Reflections and Translations 10/28/14



Date:

