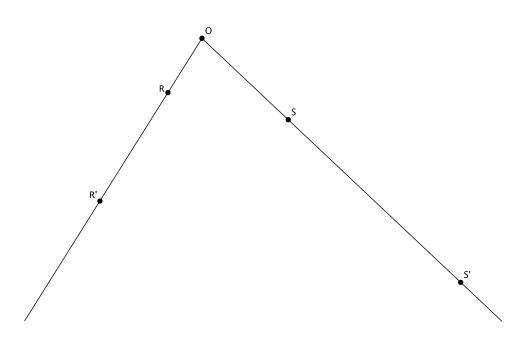
Lesson 4: Fundamental Theorem of Similarity (FTS)

Classwork

Exercise

In the diagram below, points R and S have been dilated from center O by a scale factor of r = 3.



a. If the length of |OR| = 2.3 cm, what is the length of |OR'|?

b. If the length of |OS| = 3.5 cm, what is the length of |OS'|?



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c. Connect the point R to the point S and the point R' to the point S'. What do you know about lines RS and R'S'?

d. What is the relationship between the length of segment RS and the length of segment R'S'?

e. Identify pairs of angles that are equal in measure. How do you know they are equal?





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Lesson Summary

Theorem: Given a dilation with center O and scale factor r, then for any two points P and Q in the plane so that O, P, and Q are not collinear, the lines PQ and P'Q' are parallel, where P' = Dilation(P) and Q' = Dilation(Q), and furthermore, |P'Q'| = r|PQ|.

Problem Set

- 1. Use a piece of notebook paper to verify the Fundamental Theorem of Similarity for a scale factor r that is 0 < r < 1.
 - \checkmark Mark a point *O* on the first line of notebook paper.
 - ✓ Mark the point *P* on a line several lines down from the center *O*. Draw a ray, \overrightarrow{OP} . Mark the point *P'* on the ray, and on a line of the notebook paper, closer to *O* than you placed point *P*. This ensures that you have a scale factor that is 0 < r < 1. Write your scale factor at the top of the notebook paper.
 - ✓ Draw another ray, \overrightarrow{OQ} , and mark the points Q and Q' according to your scale factor.
 - ✓ Connect points *P* and *Q*. Then, connect points *P'* and *Q'*.
 - ✓ Place a point *A* on line *PQ* between points *P* and *Q*. Draw ray \overrightarrow{OA} . Mark the point *A'* at the intersection of line *P'Q'* and ray \overrightarrow{OA} .
 - a. Are lines PQ and P'Q' parallel lines? How do you know?
 - b. Which, if any, of the following pairs of angles are equal in measure? Explain.
 - i. $\angle OPQ$ and $\angle OP'Q'$
 - ii. $\angle OAQ$ and $\angle OA'Q'$
 - iii. $\angle OAP$ and $\angle OA'P'$
 - iv. $\angle OQP$ and $\angle OQ'P'$
 - c. Which, if any, of the following statements are true? Show your work to verify or dispute each statement.
 - i. |OP'| = r|OP|
 - ii. |OQ'| = r|OQ|
 - iii. |P'A'| = r|PA|
 - iv. |A'Q'| = r|AQ|
 - d. Do you believe that the Fundamental Theorem of Similarity (FTS) is true even when the scale factor is 0 < r < 1. Explain.





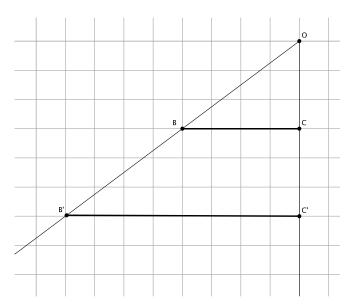
Lesson 4





- **C**' E
- 2. Caleb sketched the following diagram on graph paper. He dilated points *B* and *C* from center *O*.

- What is the scale factor r? Show your work. a.
- Verify the scale factor with a different set of segments. b.
- Which segments are parallel? How do you know? с.
- d. Which angles are equal in measure? How do you know?
- Points *B* and *C* were dilated from center *O*. 3.



- What is the scale factor r? Show your work. a.
- If the length of |OB| = 5, what is the length of |OB'|? b.
- How does the perimeter of triangle OBC compare to the perimeter of triangle OB'C'? c.
- Did the perimeter of triangle $OB'C' = r \times (\text{perimeter of triangle } OBC)$? Explain. d.



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