# **Lesson 23: The Defining Equation of a Line**

## **Classwork**

## Exploratory Challenge/Exercises 1-3

- 1. Sketch the graph of the equation 9x + 3y = 18 using intercepts. Then answer parts (a)–(f) that follow.
  - a. Sketch the graph of the equation y = -3x + 6 on the same coordinate plane.
  - b. What do you notice about the graphs of 9x + 3y = 18 and y = -3x + 6? Why do you think this is so?

c. Rewrite y = -3x + 6 in standard form.

- d. Identify the constants a, b, and c of the equation in standard form from part (c).
- e. Identify the constants of the equation 9x + 3y = 18. Note them as a', b', and c'.
- f. What do you notice about  $\frac{a'}{a}$ ,  $\frac{b'}{b}$ , and  $\frac{c'}{c}$ ?



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- 2. Sketch the graph of the equation  $y = \frac{1}{2}x + 3$  using the *y*-intercept and the slope. Then answer parts (a)–(f) that follow.
  - a. Sketch the graph of the equation 4x 8y = -24 using intercepts on the same coordinate plane.
  - b. What do you notice about the graphs of  $y = \frac{1}{2}x + 3$  and 4x 8y = -24? Why do you think this is so?

c. Rewrite  $y = \frac{1}{2}x + 3$  in standard form.

d. Identify the constants a, b, and c of the equation in standard form from part (c).

e. Identify the constants of the equation 4x - 8y = -24. Note them as a', b', and c'.

f. What do you notice about  $\frac{a'}{a}$ ,  $\frac{b'}{b}$ , and  $\frac{c'}{c}$ ?



- 3. The graphs of the equations  $y = \frac{2}{3}x 4$  and 6x 9y = 36 are the same line.
  - a. Rewrite  $y = \frac{2}{3}x 4$  in standard form.

b. Identify the constants a, b, and c of the equation in standard form from part (a).

c. Identify the constants of the equation 6x - 9y = 36. Note them as a', b', and c'.

d. What do you notice about  $\frac{a'}{a}$ ,  $\frac{b'}{b}$ , and  $\frac{c'}{c}$ ?

e. You should have noticed that each fraction was equal to the same constant. Multiply that constant by the standard form of the equation from part (a). What do you notice?



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### Exercises 4-8

4. Write three equations whose graphs are the same line as the equation 3x + 2y = 7.

5. Write three equations whose graphs are the same line as the equation  $x - 9y = \frac{3}{4}$ .

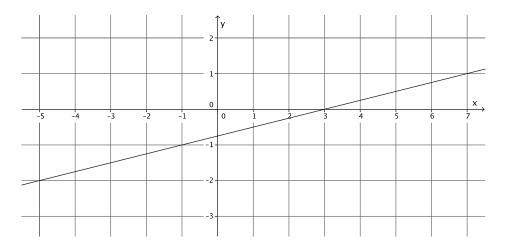
6. Write three equations whose graphs are the same line as the equation -9x + 5y = -4.



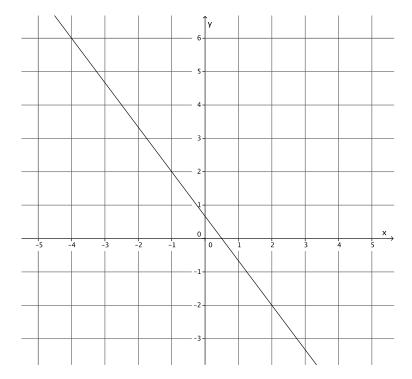
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7. Write at least two equations in the form ax + by = c whose graphs are the line shown below.



8. Write at least two equations in the form ax + by = c whose graphs are the line shown below.



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#### **Lesson Summary**

Two equations define the same line if the graphs of those two equations are the same given line. Two equations that define the same line are the same equation, just in different forms. The equations may look different (different constants, different coefficients, or different forms).

When two equations are written in standard form, ax + by = c and a'x + b'y = c', they define the same line when  $\frac{a'}{a} = \frac{b'}{b} = \frac{c'}{c}$  is true.

#### **Problem Set**

- 1. Do the equations x + y = -2 and 3x + 3y = -6 define the same line? Explain.
- 2. Do the equations  $y = -\frac{5}{4}x + 2$  and 10x + 8y = 16 define the same line? Explain.
- 3. Write an equation that would define the same line as 7x 2y = 5.
- 4. Challenge: Show that if the two lines given by ax + by = c and a'x + b'y = c' are the same when b = 0 (vertical lines), then there exists a non-zero number s, so that a' = sa, b' = sb, and c' = sc.
- 5. Challenge: Show that if the two lines given by ax + by = c and a'x + b'y = c' are the same when a = 0 (horizontal lines), then there exists a non-zero number s, so that a' = sa, b' = sb, and c' = sc.



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